

**17 July 2025**  
**University of Kaiserslautern-Landau**

# **Multidisciplinary Design Optimization for Next-Generation Sustainable Aircraft**

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Universidad Carlos III de Madrid**

- Public, young (created in 1989), and bilingual
  - *73% of degrees in English or bilingual*
  - *2<sup>nd</sup> ranked public University in Spain (Employability)*
- One of the most international:
  - *23% of students & 14% academics are foreign*
  - *51% student opted for international mobility*
  - *Incoming/outgoing students ~2000 / 2000 (1<sup>st</sup> in Spain)*
- Well-balanced from a gender perspective:
  - undergraduates: 54% women / 46% men
- Mid-size:

■ undergraduate:	17.000
■ graduate:	5.500
■ academic staff:	2.000



4 campuses in Madrid region

Leganés: **School of Engineering (EPS)**

~45% of UC3M

20 undergraduate degrees

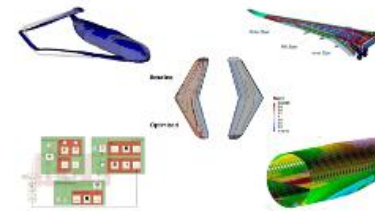
39 master degrees

11 PhD programs

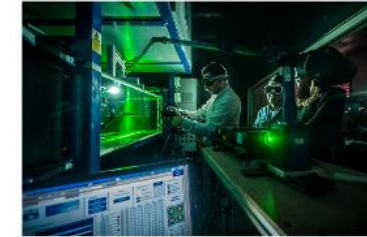
# UC3M - Aerospace Engineering Department

- Born in **2010**
- **13** Permanent Professors (35% non-Spanish)
- **~75 people** (counting also Assistant prof., Post-Docs & PhDs students)
- Recognized with prestigious grants/awards:
  - **3 ERC StG** (European Research Council)
  - **1 Ramon y Cajal Fellowship** (Spanish Government)
  - **1 Senior Beatriz Galindo Fellowship** (Spanish Government)
  - **3 Leonardo Grants** (BBVA Foundation)/
- Covering **6** research areas

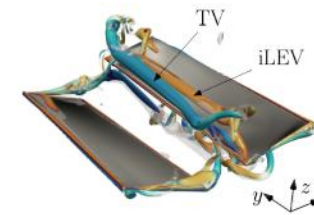
Aeroelastic and Structural Design Lab (ASDLab)



Experimental Aerodynamics and Propulsion Lab



Computational Fluid Dynamics Lab



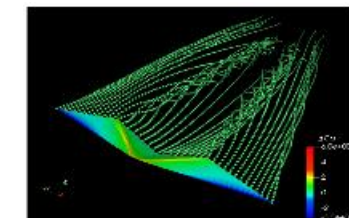
Plasma and Space Propulsion Team (EP2)



Dynamics and Control in Aerospace Systems



Tethers Applied to Aerospace Engineering



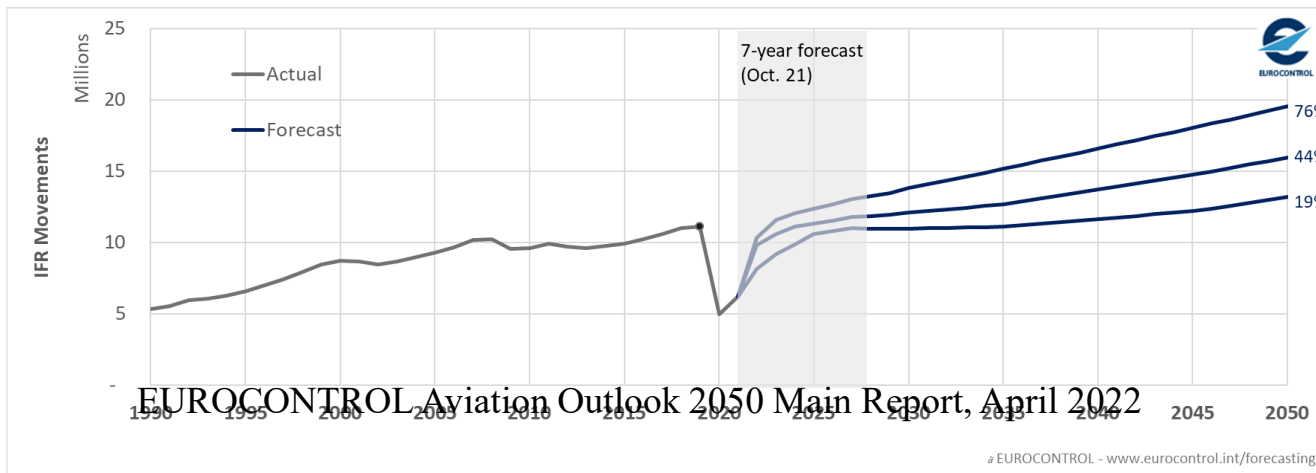
1. Presentation (UC3M, Aerospace Engineering Department,...)
2. Motivation for Sustainable Aviation
3. MDO for sustainable aviation. Applications
  - a. Hybrid-electric Large Aspect Ratio Wings
  - b. Highly flexible wings

- Air traffic has **rebounded**: 2024 flights at **96% of 2019** levels, emissions at **98%**
- 2025 emissions are projected to exceed 2019 levels (**↑4%**).
- Forecast: **+40% flights** by 2050 in Europe (~15.4 million flights).
- Aviation contributes **~4% of EU GHG**, **~13.9% of transport emissions**, but **non-CO<sub>2</sub> effects** double its climate impact
- Despite efficiency gains, CO<sub>2</sub> per passenger-km down only **~1–2% per year**.

**30-YEAR  
FORECAST  
2022-2050**

**16 MILLION  
FLIGHTS BY 2050**  
(RANGE: 13.2-19.6 MILLION)  
**UP 44% ON 2019**

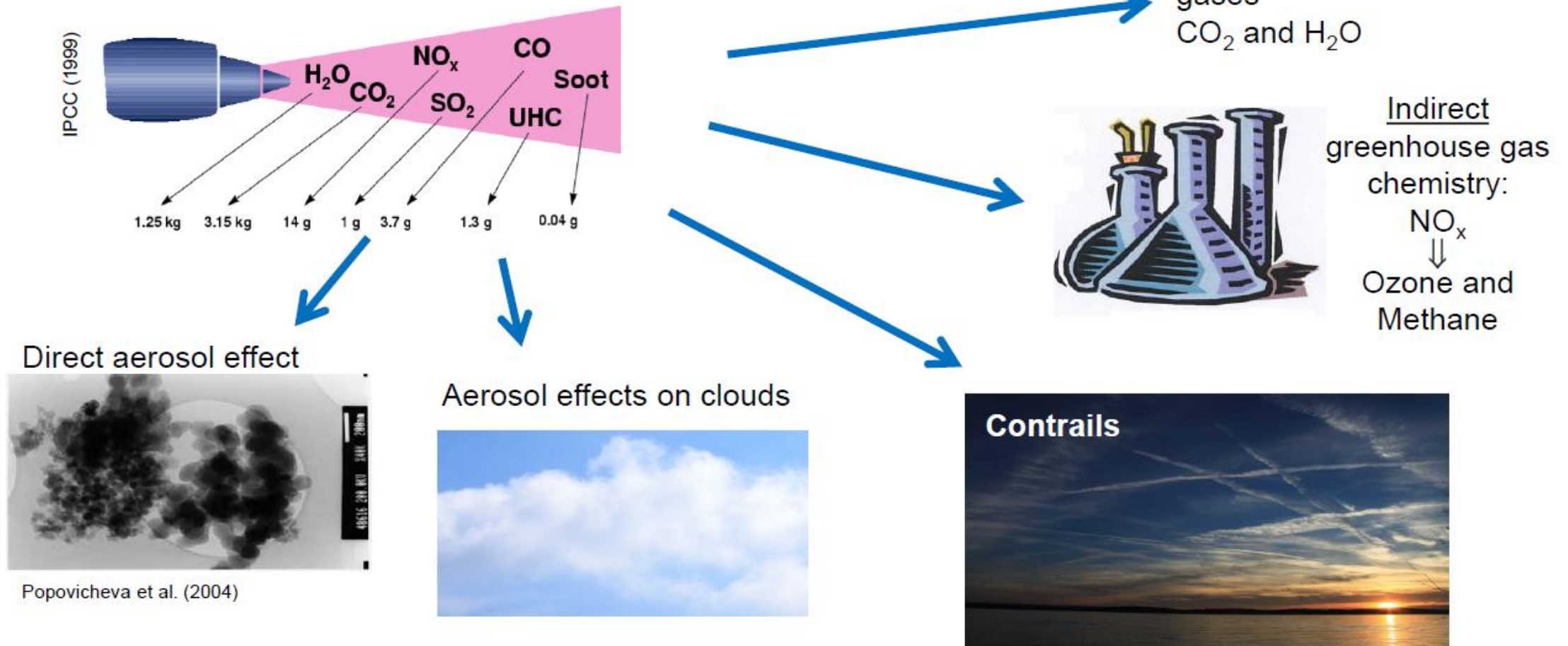
- **10-YEAR LAG** SINCE PREVIOUS LONG-TERM FORECAST (2018).
- **MIDDLE-EAST & ASIA/PACIFIC**: MOST DYNAMIC FLOWS WITH ECAC BY 2050.



## Need to act fast

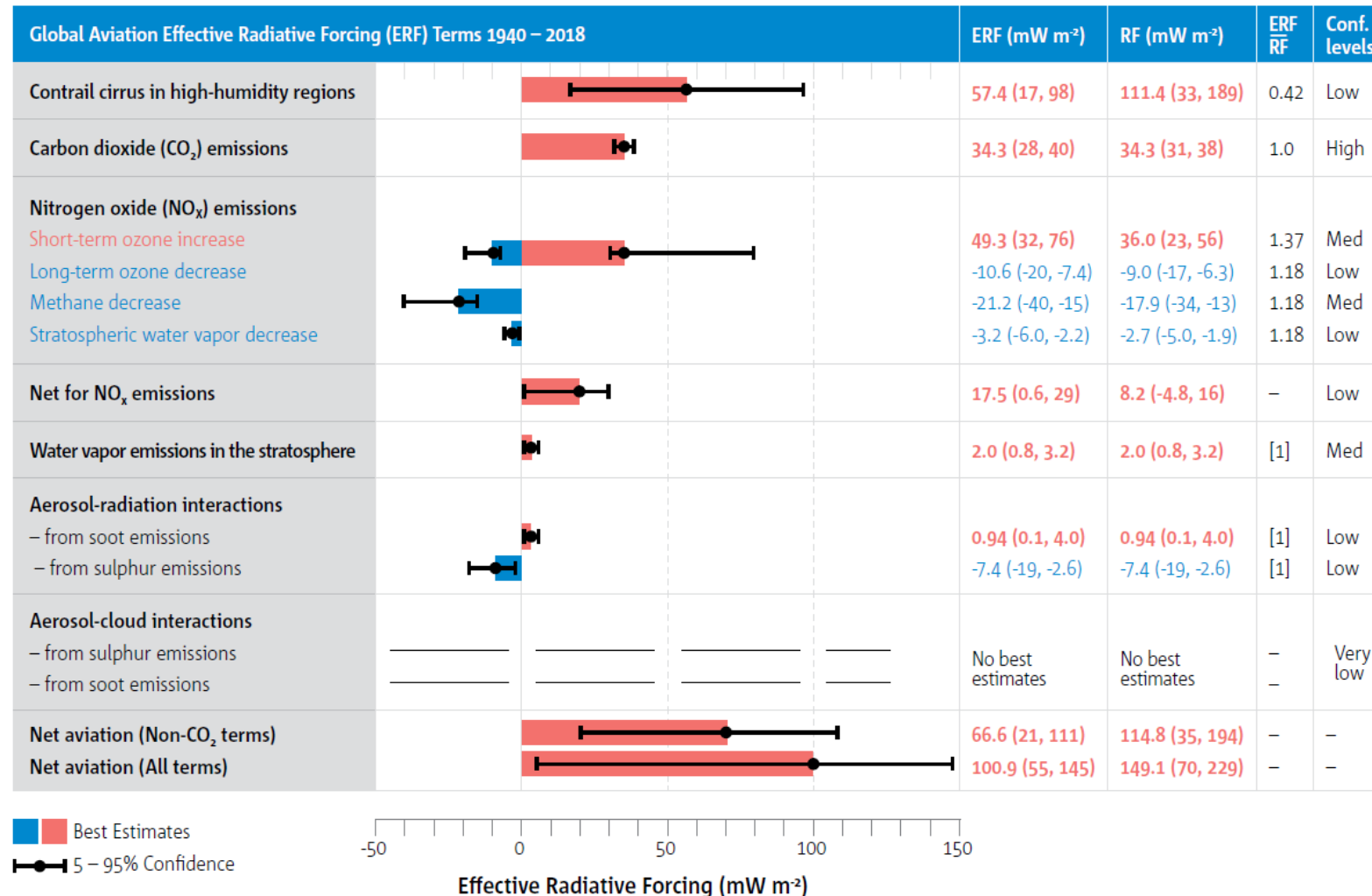
If some **intermediate goals** are not implemented immediately and **achieved by 2030**, the opportunity for transformation will slip away, leaving the world to face the escalating climate impacts of a rapidly growing aviation sector, which is projected to at least double by 2050.

## Climate Effects of Aviation Emissions



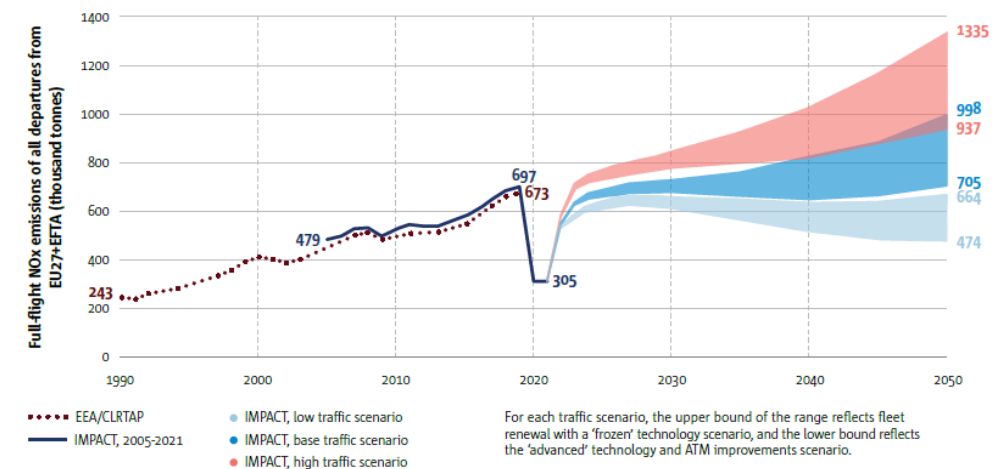
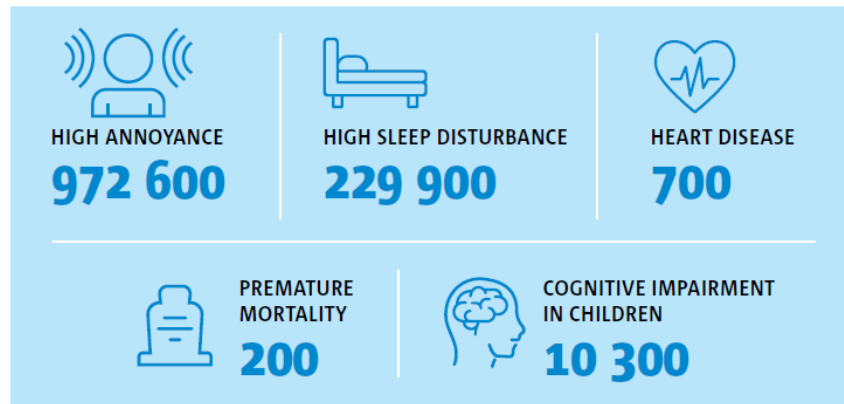


**non-CO<sub>2</sub>** emissions represent the largest fraction of the total ERF of aviation, at present, **although** the level of uncertainties from the non-CO<sub>2</sub> effects is 8 times larger than that from CO<sub>2</sub>, and the overall confidence levels of the largest non-CO<sub>2</sub> effects are ‘low’.



## Three main aspects

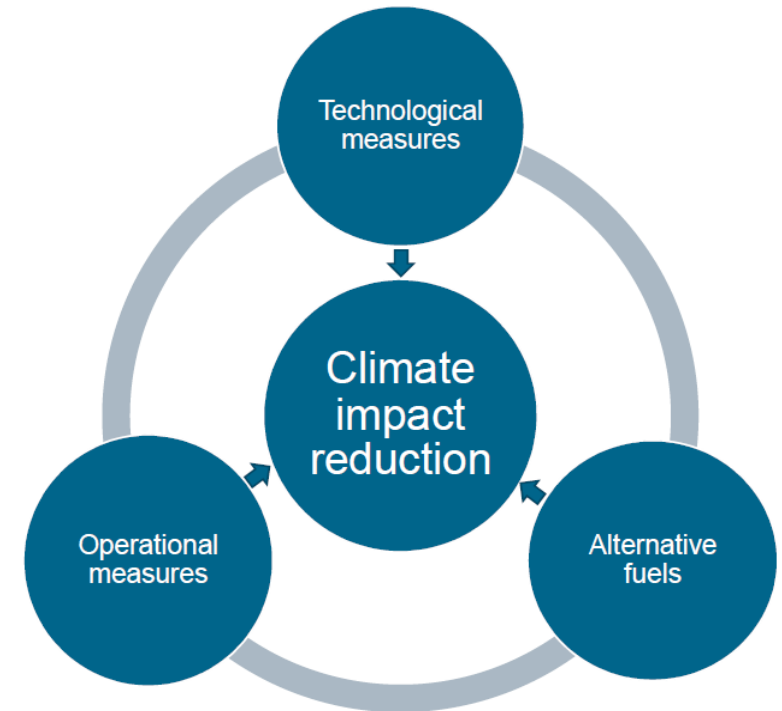
- Climate change
- Two aspects related to “direct” effects on population living close to airports. Concept of LAQN (Local Air Quality and Noise)
  - **Local Air Quality (LAQ)**
  - **Noise**





**Sustainable aviation** focuses on minimizing the environmental impact of air travel by adopting

- **Advanced technologies**
  - **Replace old aircraft of fleets**
  - **Next generation aircraft (disruptive technology)**
- **Alternative fuels, and**
- **Efficient operations**
  - Ground/Flight operations
  - ATC efficiency
  - Exploring innovative technologies like **electric and hydrogen** propulsion.





## Clean Aviation's aircraft concepts

Entry-Into-Service in 2035



Ultra-efficient  
Regional aircraft

-30%  
CO<sub>2</sub>\*

-86%  
CO<sub>2</sub>\*  
incl. SAF



Hydrogen powered  
aircraft

-100%  
CO<sub>2</sub>\*



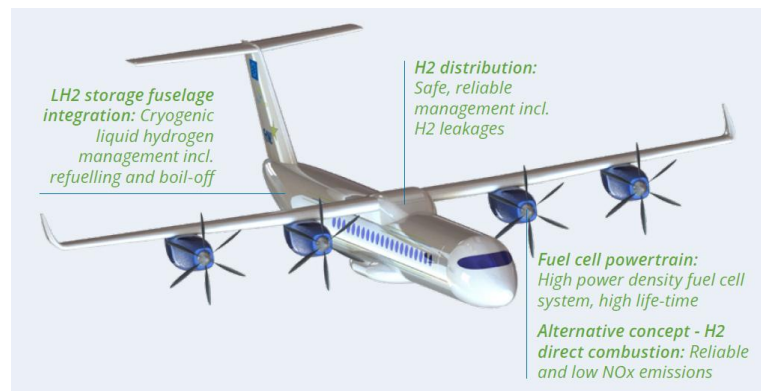
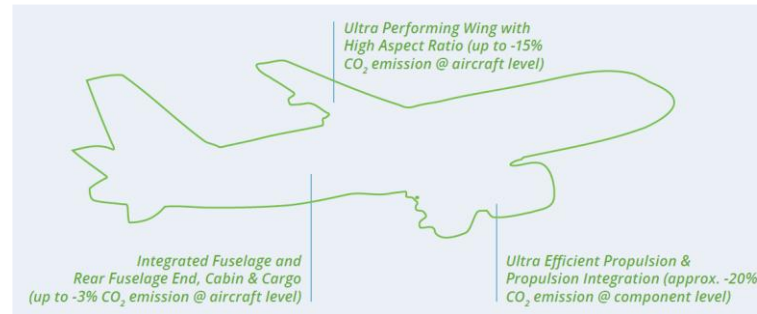
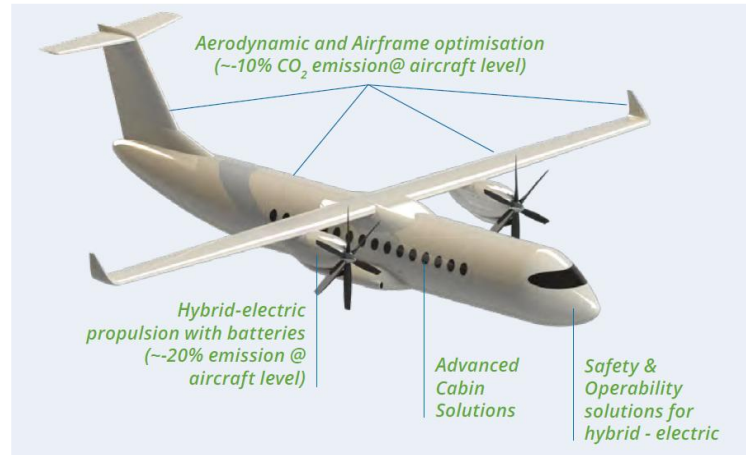
Ultra-efficient Short and  
Medium Range aircraft

-30%  
CO<sub>2</sub>\*

-86%  
CO<sub>2</sub>\*  
incl. SAF

\* non-CO<sub>2</sub> effects not yet quantified

- Decarbonization goals demand **disruptive architectures**
  - hybrid-electric, hydrogen
  - novel configurations
- **Break with legacy**
  - no historical data
  - no baseline designs
  - Multiple **tightly coupled** disciplines
    - Aerodynamics, structures, propulsion, thermal management, systems, ...
- **Sustainability** adds new **dimensions**:
  - emissions, energy
  - lifecycle
  - regulatory constraints.



In hybrid-electric systems, propulsion sizing depends

- on thermal management,
- which in turn affects weight and drag.

H<sub>2</sub> aircraft, the LH<sub>2</sub> tank volume and placement impact

- the aerodynamic shape,
- center of gravity, and
- structural layout simultaneously.

No Historical Data = Need for Physics-Based, Integrated Models

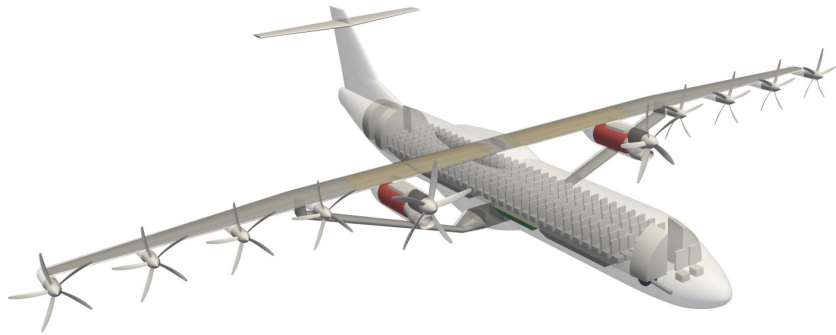
- Legacy aircraft had empirical decoupling
  - *"this works because it always worked."*
- Disruptive aircraft lack validated trends
  - models must be fully coupled
  - and physics-based from the start
- Optimization must happen in this complex, high-dimensional space
  - enter MDO.

While aircraft have always required coordination between disciplines, disruptive designs amplify these dependencies to the point where **traditional sequential approaches become insufficient.**

MDO isn't new, what's new is that **it's now indispensable.** Legacy aircraft "tolerated" approximation. Sustainable aircraft, with tight energy and emission constraints, do not.

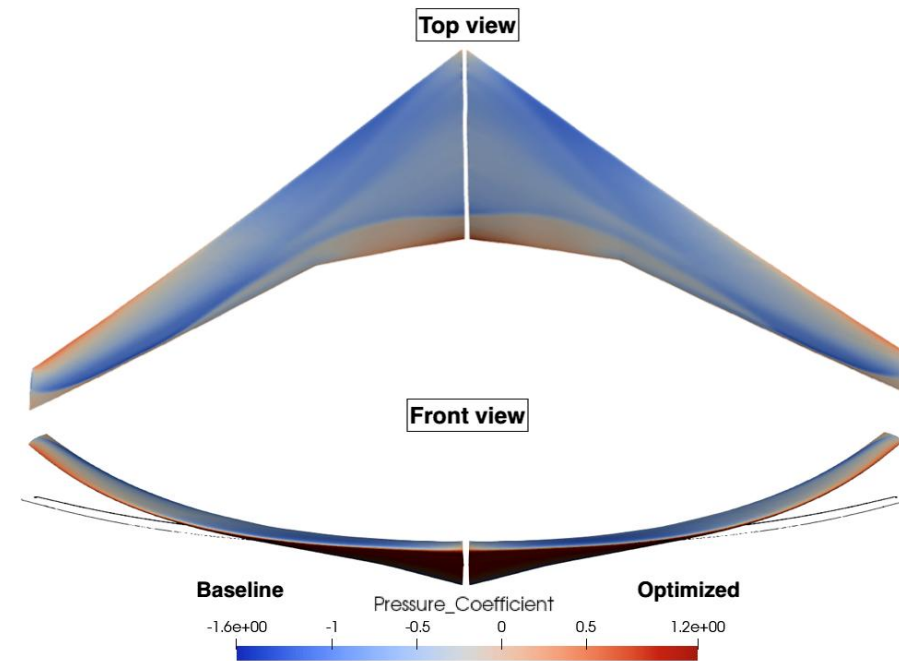
## Application 1

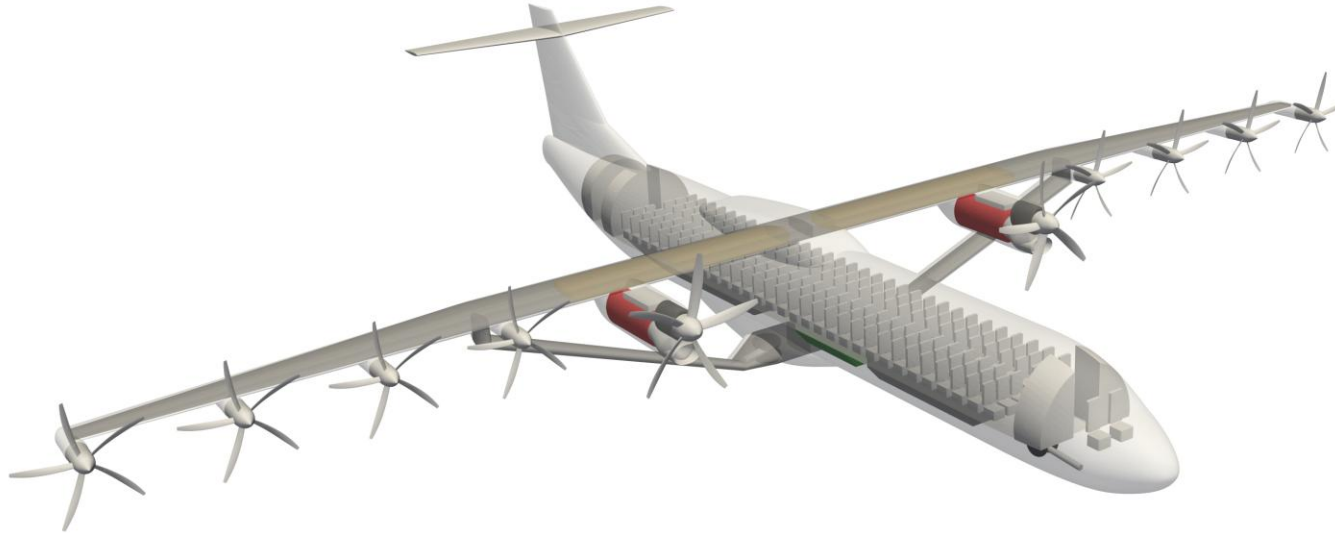
- Improving Local Air Quality and Noise
- Hybrid-electric powertrain
- Strut-braced wing
- New Operations (trajectories)



## Application 2

- Highly-flexible wings
  - Emission reduction







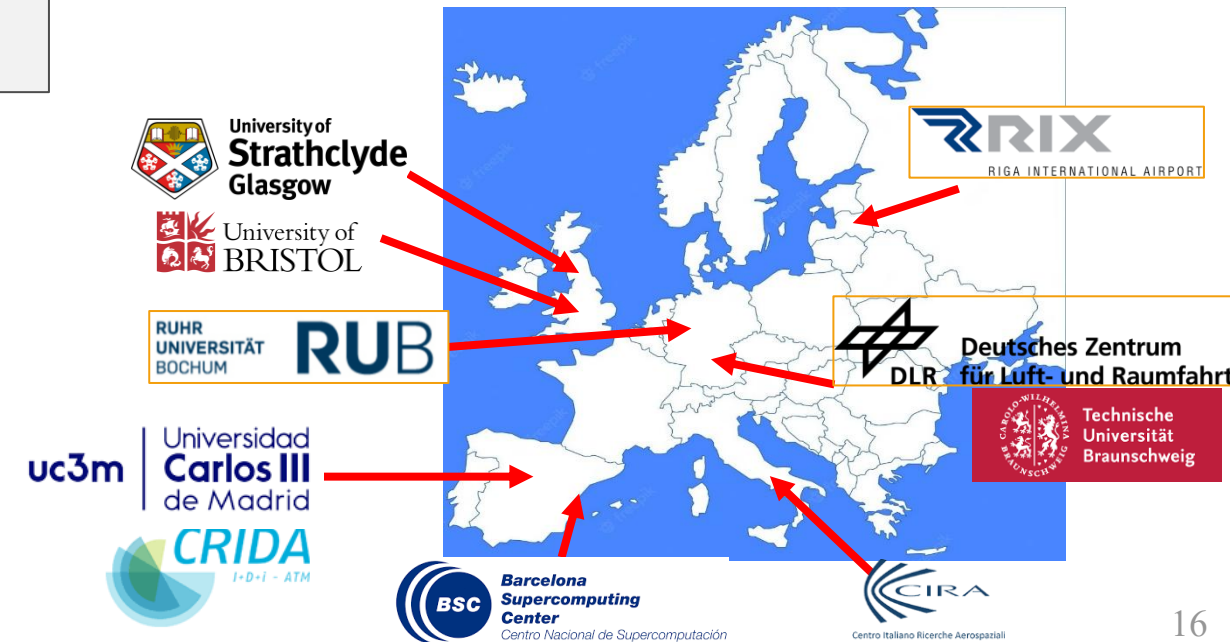
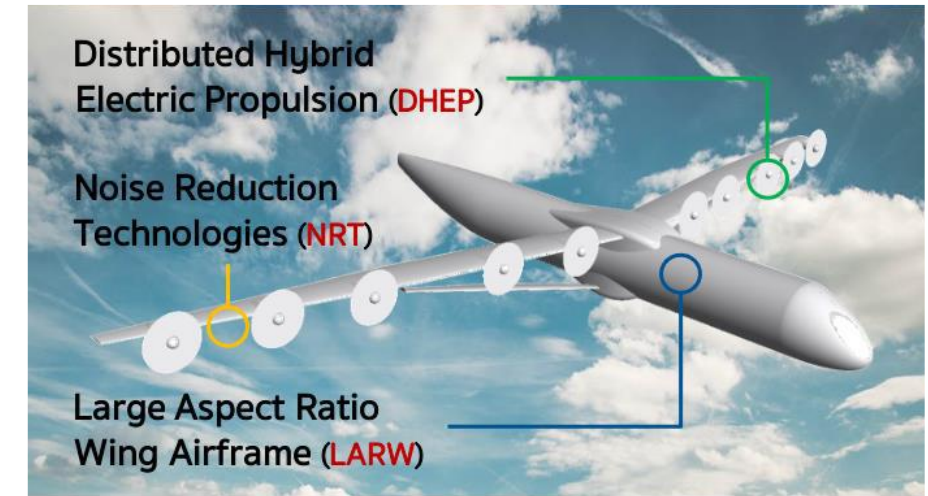
# HORIZON-CL5-2022-D5-01-12: Towards a silent and ultra-low local air pollution aircraft

- “Deliver **transformative technologies** that will allow a step change in the reduction of **local air quality (LAQ)** impact below 900m above ground level around airports”
- “Deliver transformative technologies towards a **silent aircraft operations around airports**” (**NOISE**)

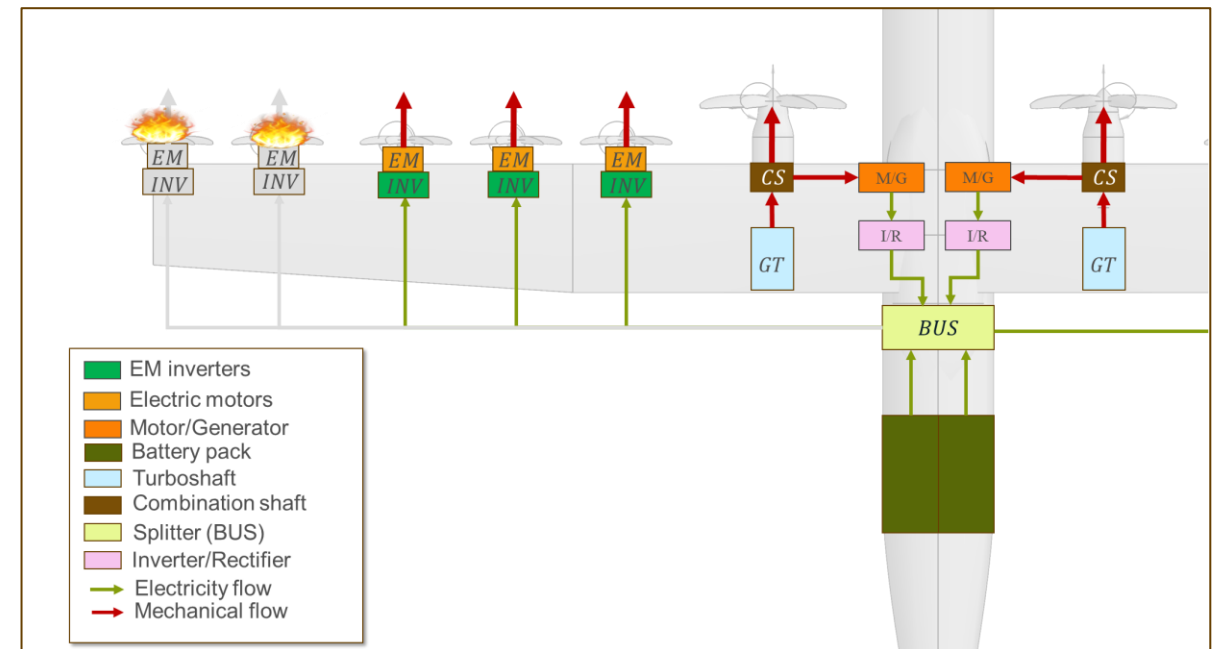
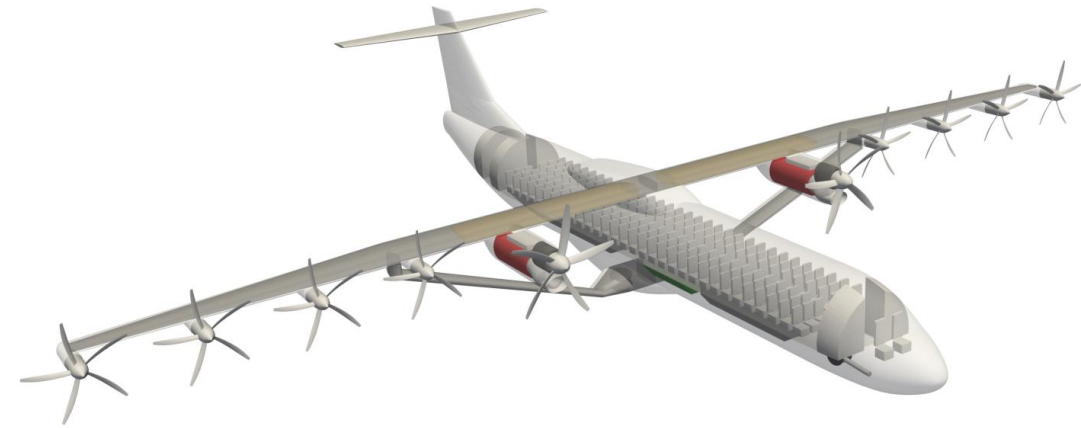
## INDIGO

*INtegration and Digital demonstration of low-emission aircraft technologies and airport Operations*

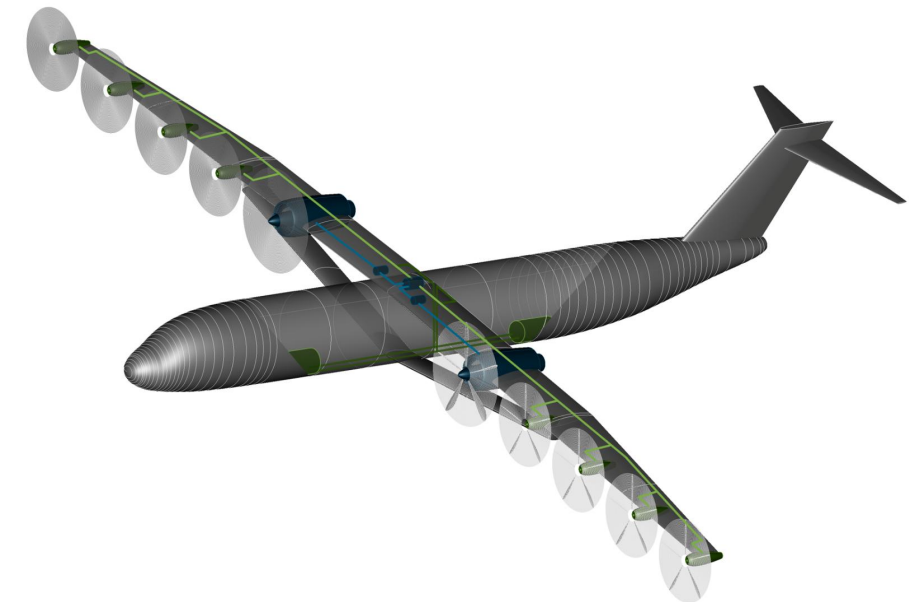
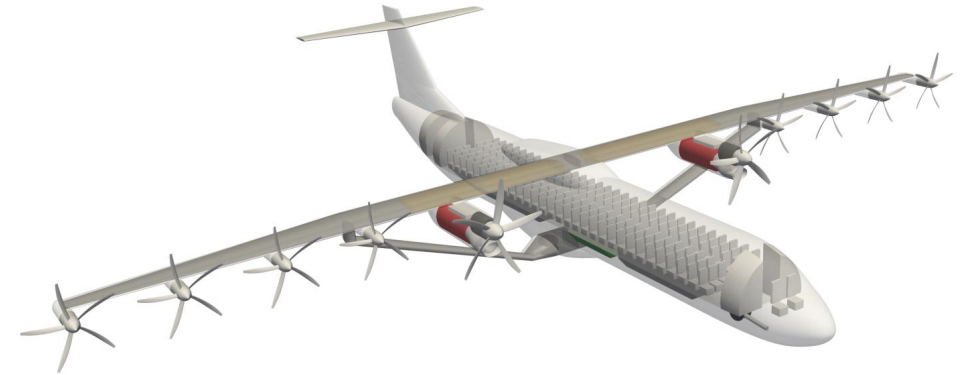
- 10 partners (8 beneficiaries + 2 associated).
- Total funding 4.4m€ (EU funding 3,1 m€ + UKRI 1,3 m€)
- 7 WPs , 15 Deliverables; 36 months



- Introduction
- Methodology
- Optimization campaign

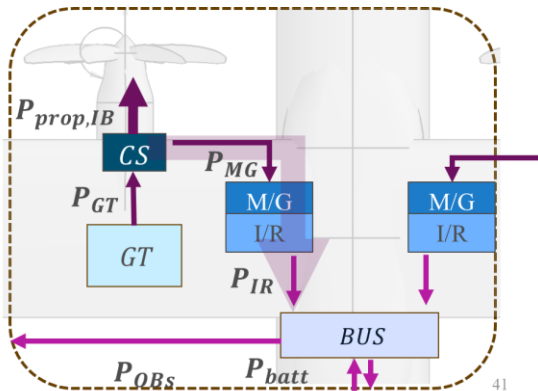
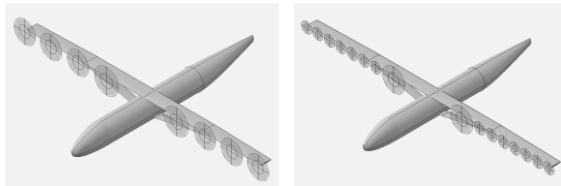


- **Large Aspect Ratio Wings (LARW)**
  - **Strut-braced wing** aircraft
  - Offers possible better integration of DHEP
- **Hybrid Electric Propulsion**
  - Go as **electric** as possible below 900m
  - Electric technologies still lagging for **full electric** trips (for MTOW of A320 and design range 1000nm)
  - Many powertrain architectures (serial, parallel)
- **Distributed Electric Propulsion (DEP)**
  - Synergistic with noise reduction
  - Blowing effects



## Deliverable 1.1

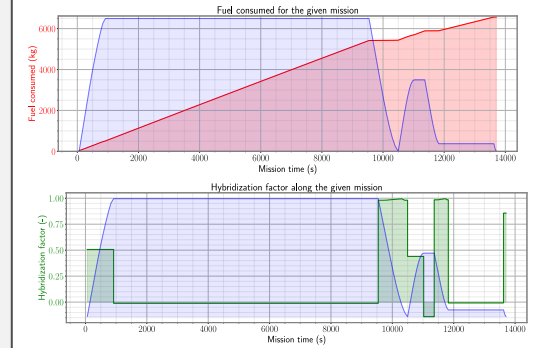
Provide an interim LARW-DHEP baseline



- How many propellers?
- Which powertrain architecture?
- Battery capacity?
- How to distribute the 2 sources of energy along the mission?
- Wing planform to integrate better the DHEP
- How to balance conflicting needs (LAQN vs block fuel)
- Technology uncertainties and robust design
- Minimize impact on surroundings on real trajectories

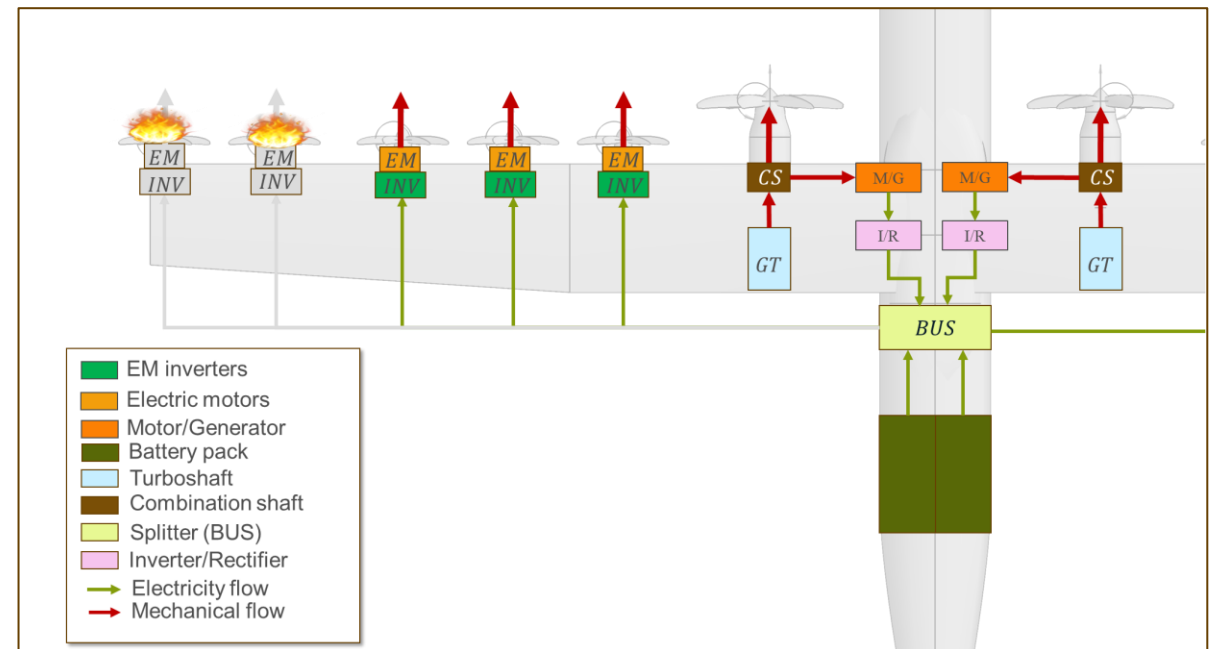
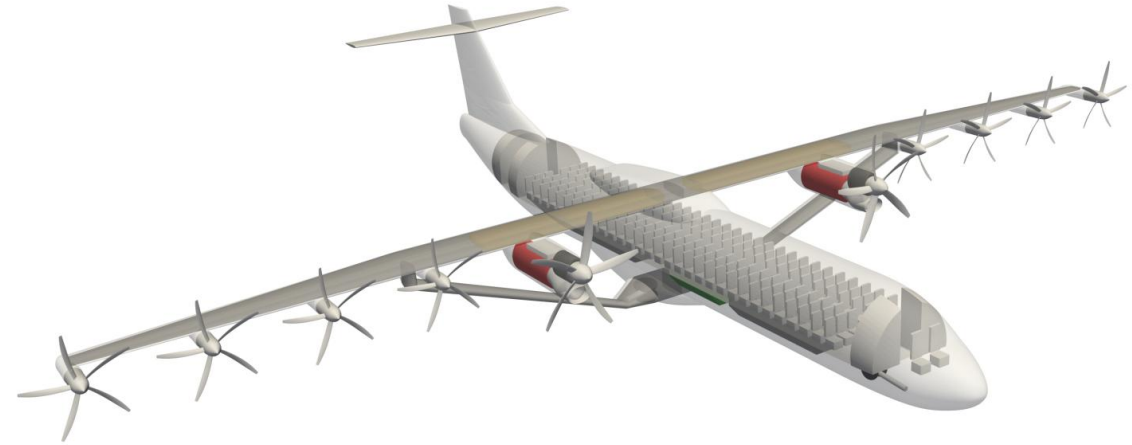
## Deliverable 5.1

Preliminary design under Uncertainties



MDO

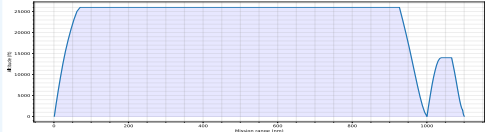
- Introduction
- **Methodology**
- Optimization campaign
- Results



## MDAO platform (MOTIVATION - Mdao fOr susTaInable aViATION)

## TLDR

## Mission and range



## Design variables

- Component ratings
- Prop diameters and RPM
- Wing planform
- Hybridization factor/thrust splitting

## Design constraints

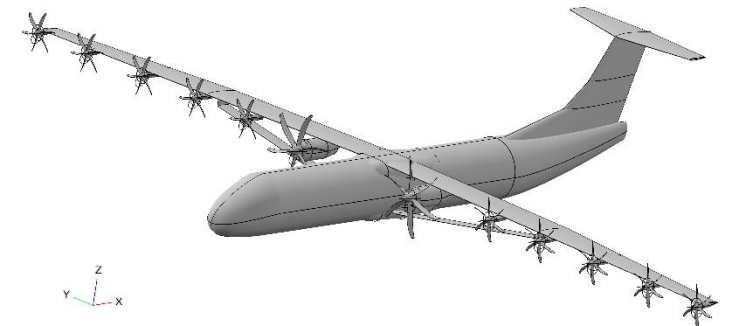
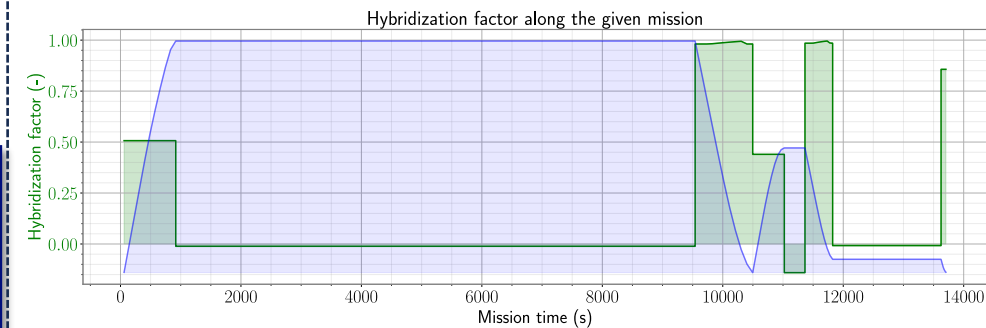
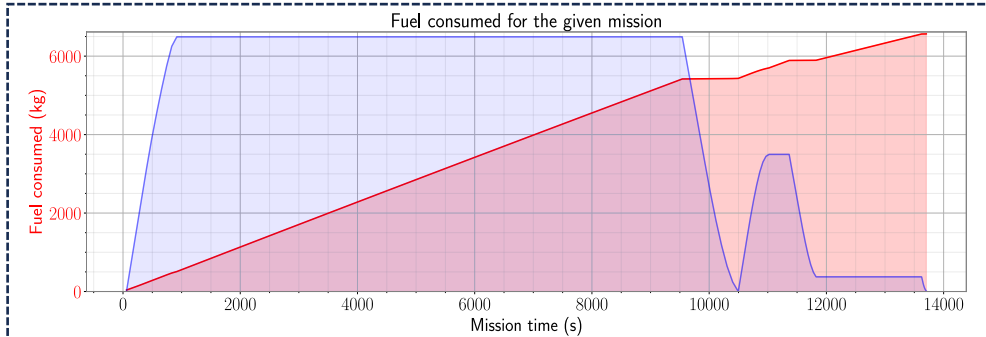
- Sizing margins
- Throttles (Gas turbine and Electric motors)
- Battery residual SOC
- Propellers gaps
- TOFL and RLD
- OEI Certification gradients

Objective function(s)  
 $\min \Phi_i(x)$

MOTIVATION



- Forked from *OpenConcept* (2019)
- **Flexibility:**
  - different powertrains
  - discipline modules (fidelity)
- **Powerful:**
  - large optimization problems
  - avoiding a-priori decisions (extremely important as legacy-experience is missing).

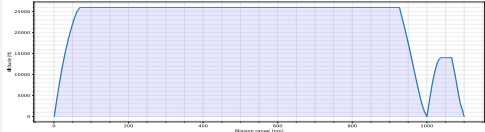




## MDAO platform (TOPAZ - Tool for Optimizing Powerplants and Aircraft with Zero-emissions)

## TLDR

## Mission and range



## Design variables

## As before +

- Htp/Vtp sizing, wing positioning

## Design constraints

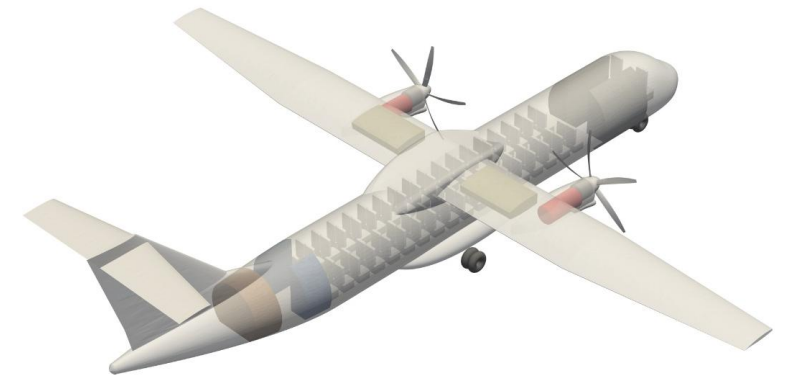
## As before +

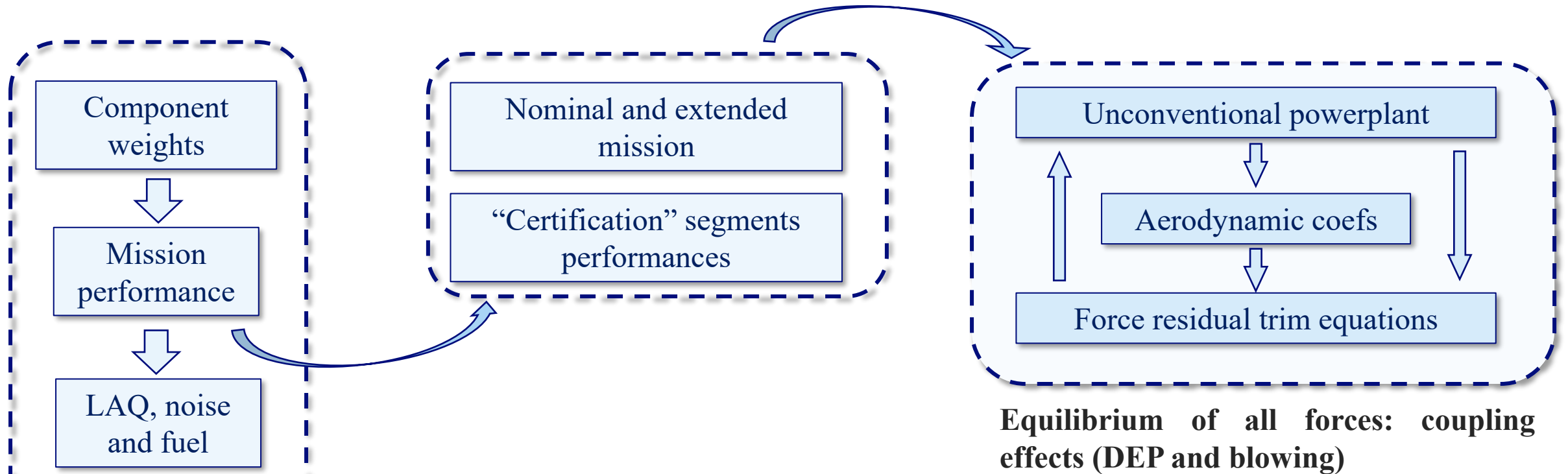
- Volume (integration of batteries)
- Trim (high-low speed)
- Stability
- Thermal management

Objective function(s)  
 $\min \Phi_i(x)$

GEMSEO

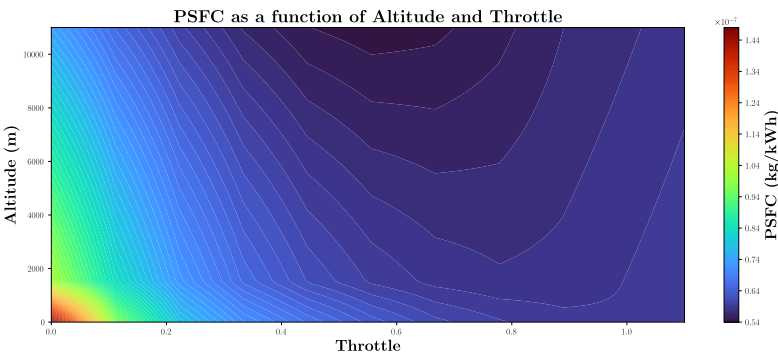
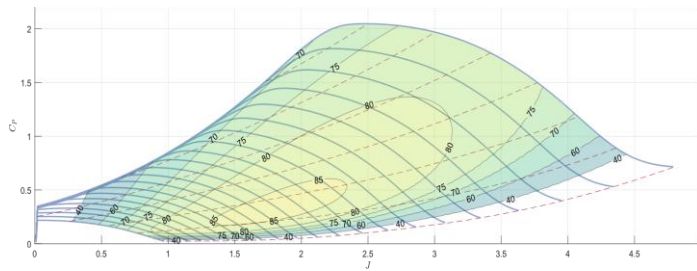
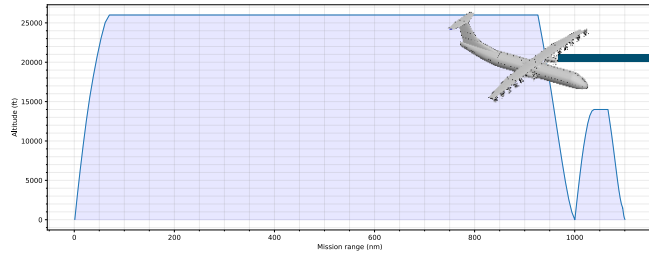
- **Flexibility:**
  - different powertrains
  - discipline modules (fidelity)
- **Powerful:**
  - large optimization problems
  - avoiding a-priori decisions (extremely important as legacy-experience is missing).
- JAX-AD for sensitivities





- WP1 - Use “**minimal**” fidelity models for large design space exploration
- WP5 - Use “**mid/high-fidelity**” models on a reduced design space. Uncertainties.
- Define the mission as **FAR/CS25 compliant**, considering takeoff, landing and certification segments (climb gradients) – **Regulations yet to be defined for hybrid-electric aircraft!**
- Solve the **strong couplings** from the introduction of new technologies.

## Convergence of residual

 $HF, \psi$ 

$$\mathcal{R}_{vertical} = W \cdot \cos(\gamma) - q \cdot S_{ref} \cdot (CL_{\alpha} \cdot \alpha + CL_0)$$

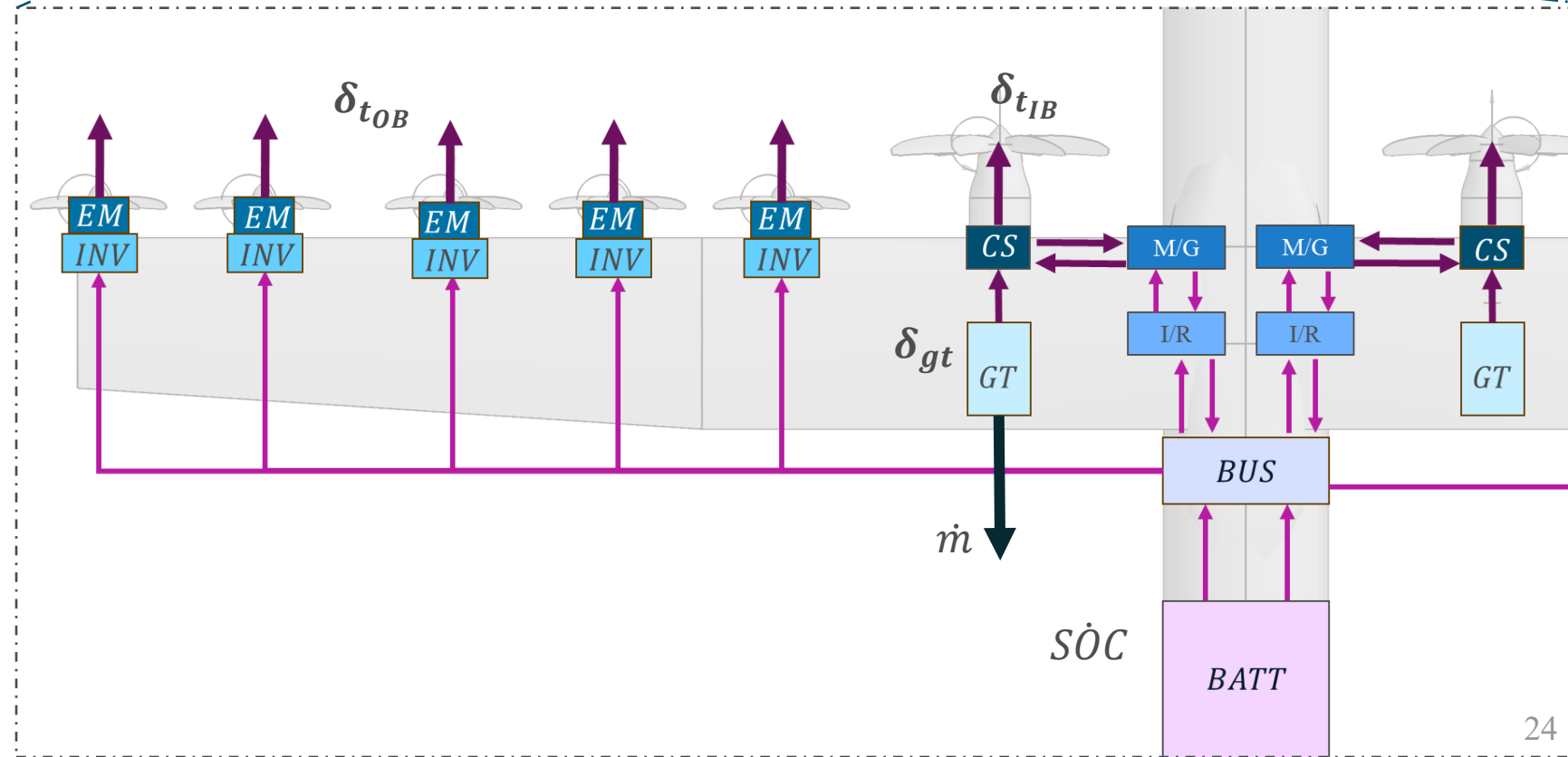
$$\mathcal{R}_{horizontal} = T - W \cdot \sin(\gamma) - q \cdot S_{ref} \cdot (CD_0 + CD_{\alpha} \cdot \alpha + CD_{\alpha\alpha} \cdot \alpha^2)$$

throttles  
 $\delta_{t_{OB}}$   $\delta_{gt}$   $\delta_{t_{IB}}$

$\dot{m}$   
 $SOC$

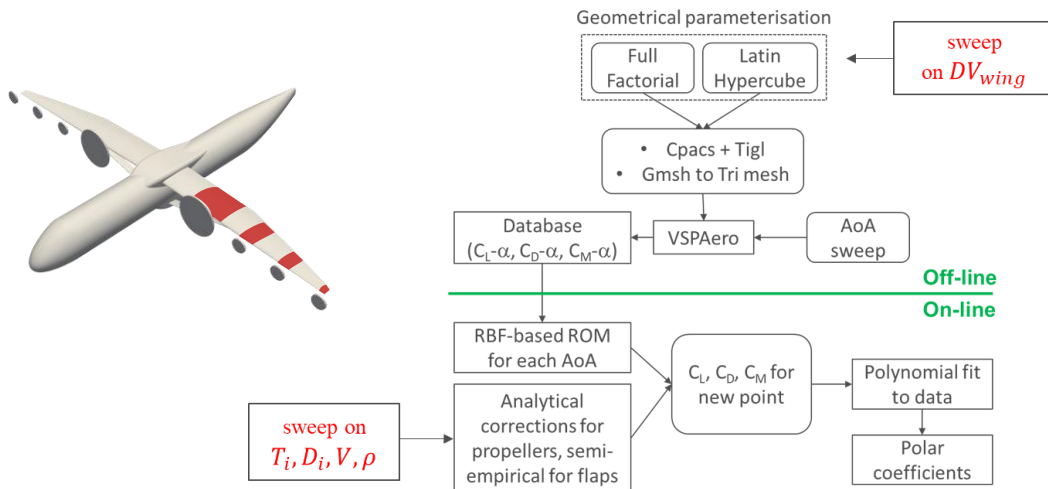
tighter coupling

Powerplant



## Low-fi

- ROM
  - VLM ( VSPAero)
  - Analytical correction for propeller blowing
  - Semi-empirical equations for flap, etc...

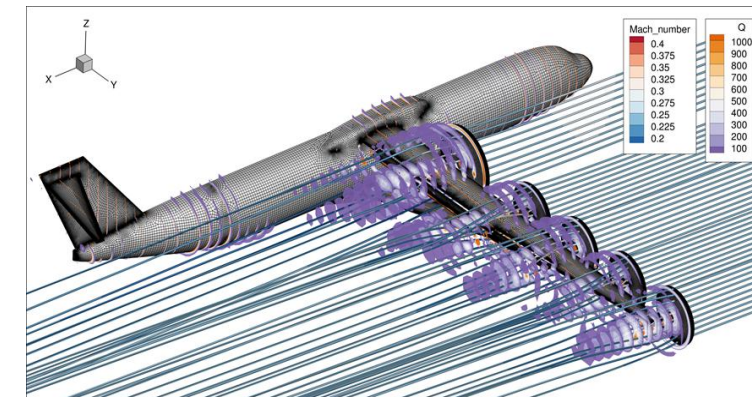
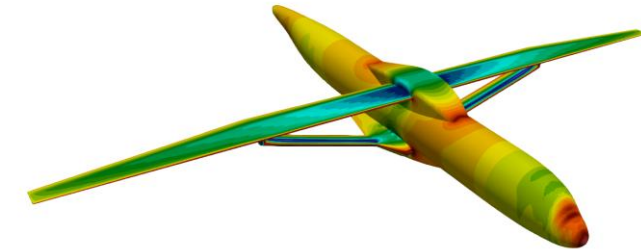
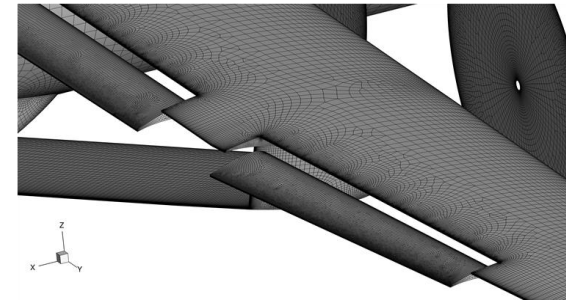


$$\begin{cases} C_L = C_{L_0} + C_{L_\alpha} \alpha \\ C_D = C_{D_0} + C_{D_\alpha} \alpha + C_{D_{\alpha\alpha}} \alpha^2 \\ C_m = C_{m_0} + C_{m_\alpha} \alpha + C_{m_{\alpha\alpha}} \alpha^2 \end{cases}$$

$$C_{L_x}, C_{D_x} = f(DV_{wing}, T_i, D_i, V, \rho)$$

## High-fi

- Multi-fi Surrogate Model (SM)
  - Hi-fi SU2+TAU
  - 6 SM for 6 polars (2 high-speed, 3 Low-speed)
  - Propeller blowing



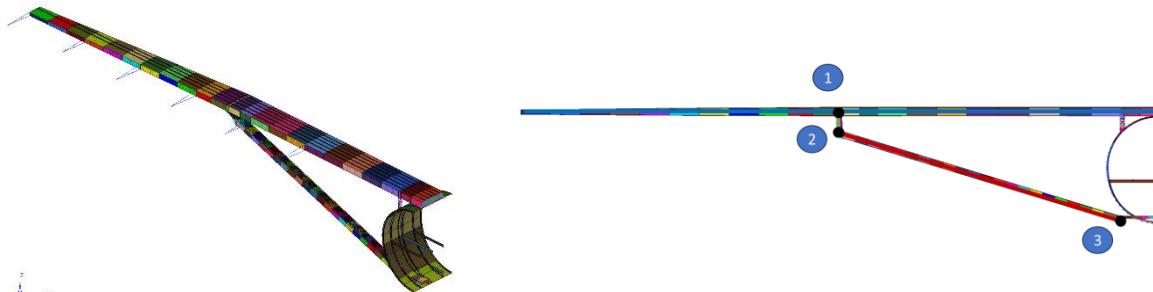
Flight Case Visualization (not trimmed), Starting Point for Trim Routine

## Low-fi

- Weight breakdown
- Classic semi-empirical formula, FLOPS.  
However,
  - Structural weight: coefficients calibration based on gFEM structural sizing (optimization)
  - Weight of powerplant system as regression on Max Power – Weight curves [RUB, UST, TUBS]

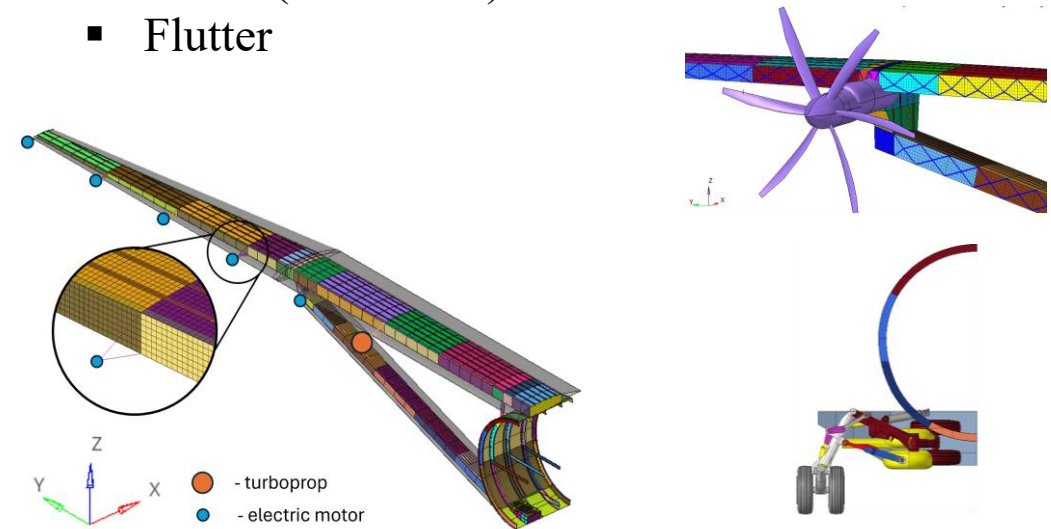
$$W = OEW + W_{PL} + W_F + W_{batt}$$

$$OEW = W_{struct} + W_{sys} + W_{furnishing} + W_{operitems} + W_{ppsys}$$

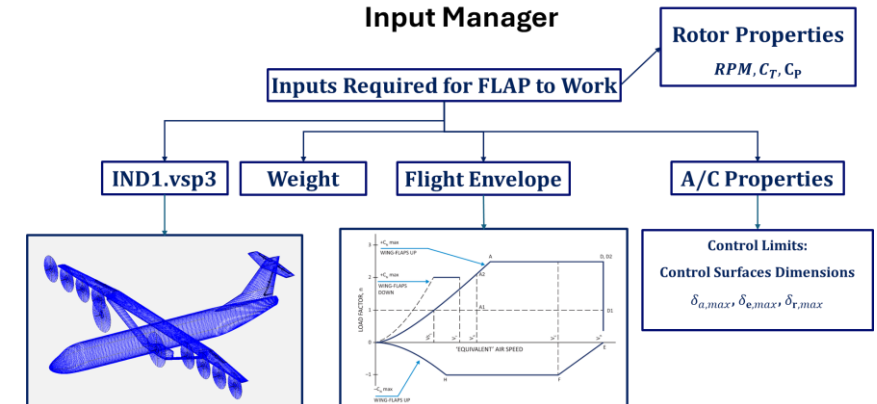


## High-fi

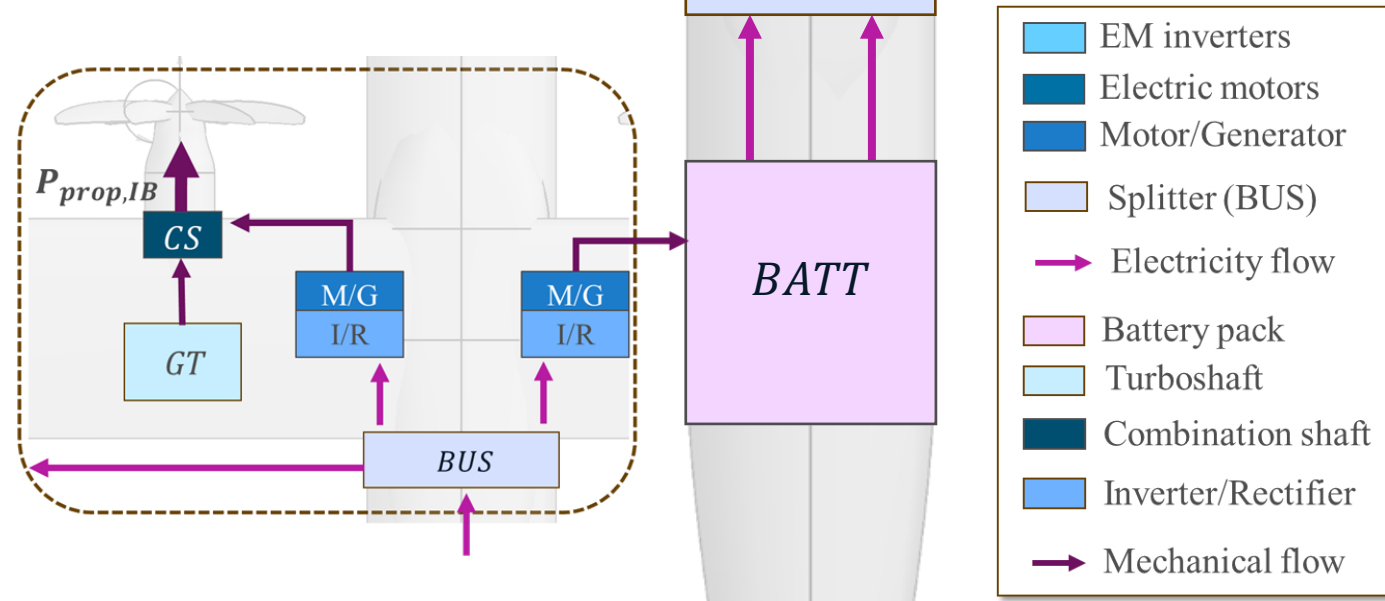
- SM for lifting system weight
- gFEM
  - Loads (bookcases)
  - Flutter



## Input Manager



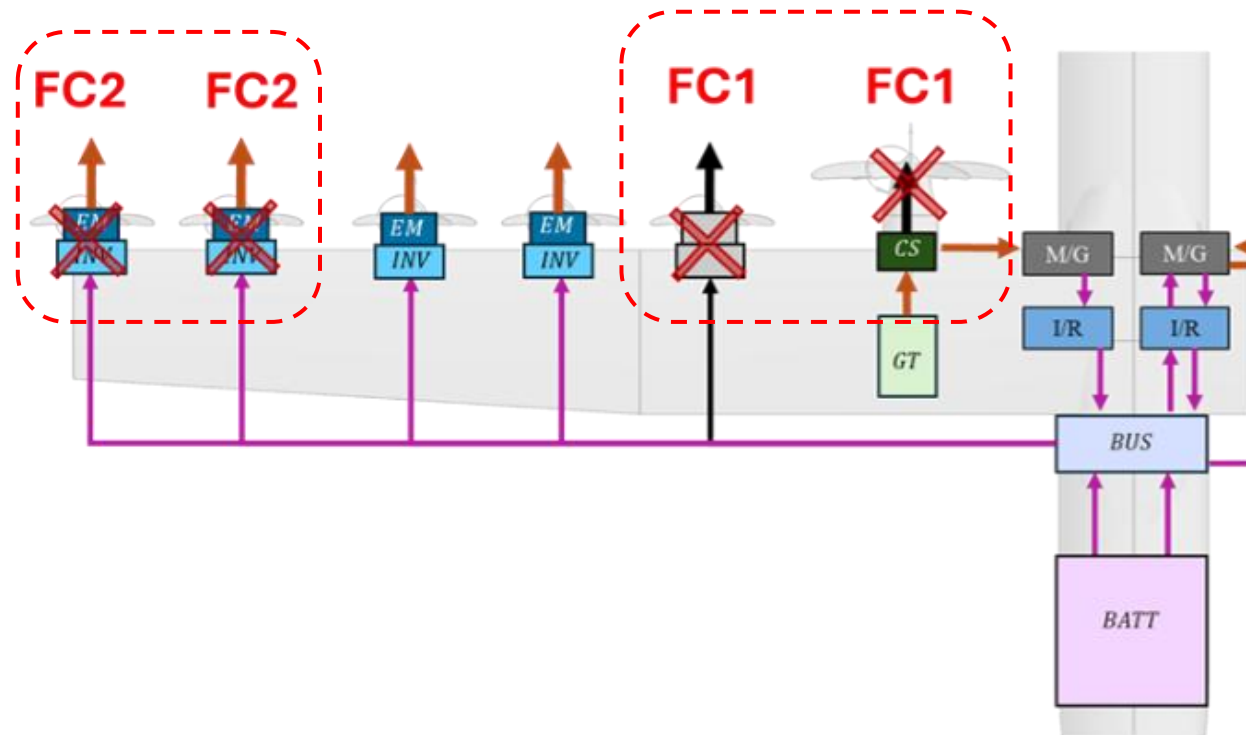






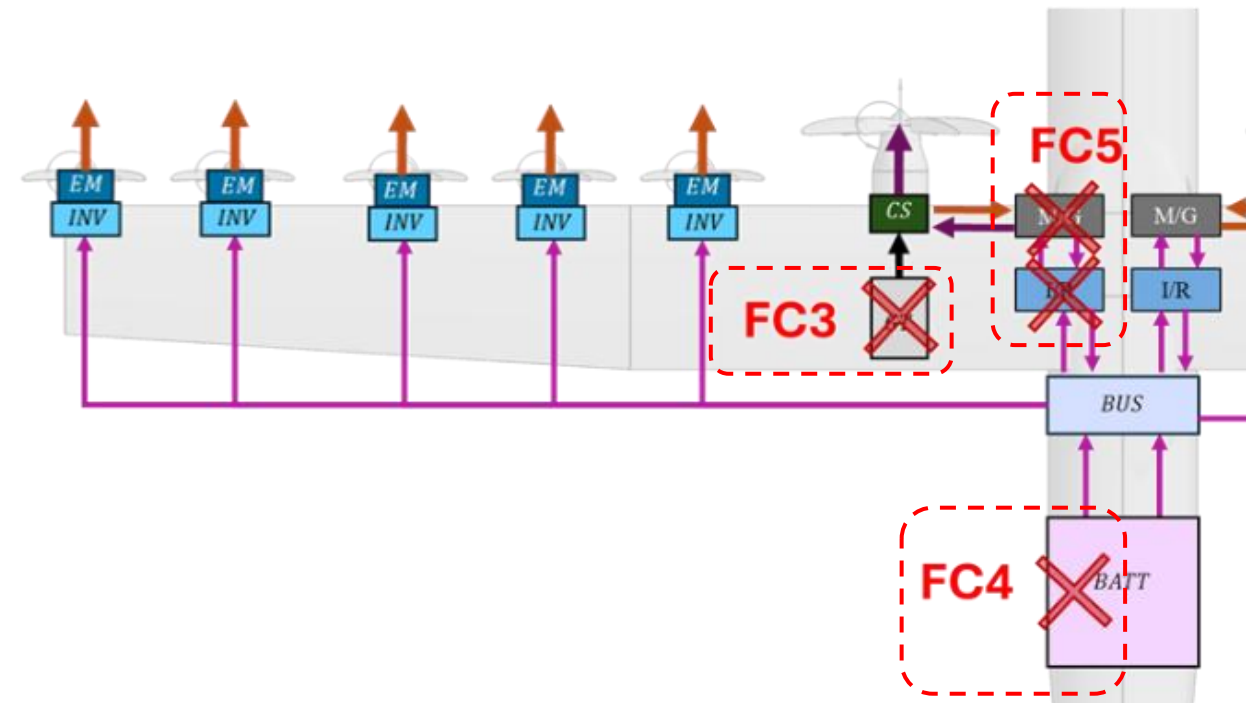
## Lack of Thrust

- FC1 - 2 most-inboard propellers
- FC2 - 2 most-outboard propellers

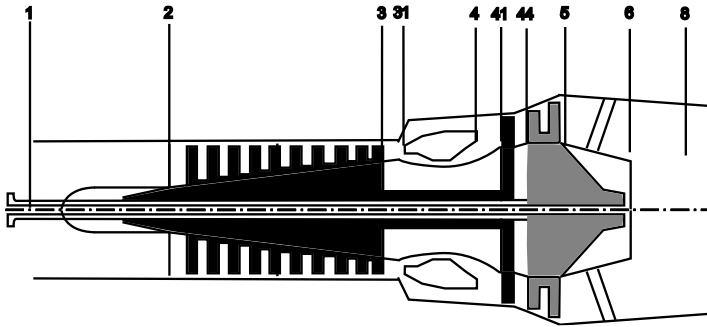


## Lack of Power

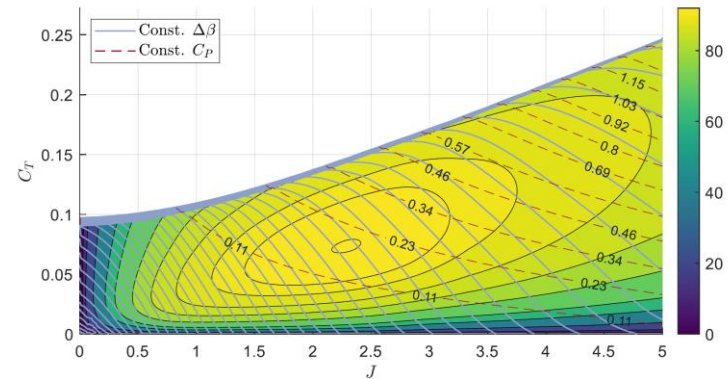
- FC3 – 1 Gas Turbine Out
- FC4 – 50% Battery pack Out
- FC5 – 1 Electric Motor/Generator Out



## Gas Turbine (TUBS/RUB)



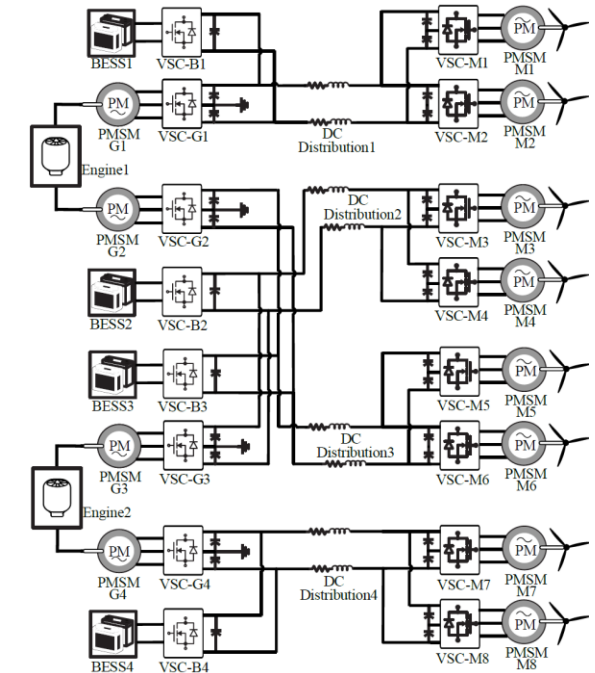
## Propeller Aerodynamics (TUBS)



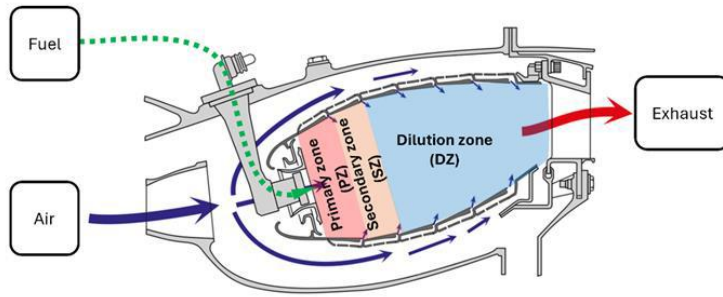
## Electric Power System (UST)

For a certain power profile

- Sizes electric system
- Outputs weight, efficiencies
- Includes transient-simulation and failure rates



## Combustion Chamber (RUB)



For a certain power profile

- Sizes the thermal components
- Evaluate weight, PSFC
- $NO_x$ ,  $CO$ ,  $HC$ ,  $PM$ ..

For a certain thrust profile

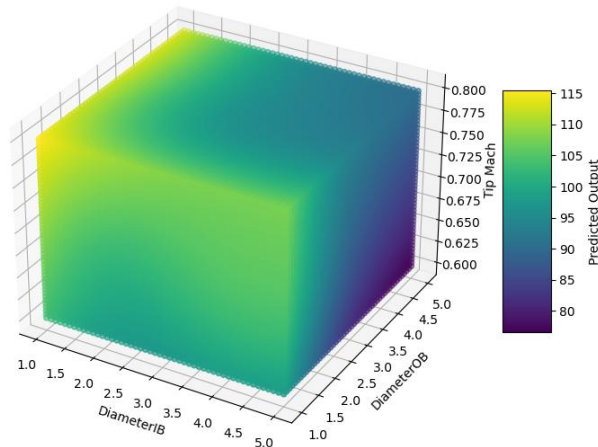
- Sizes the propellers
- Different Disk loadings

**All given as SMs**

## Low-fi

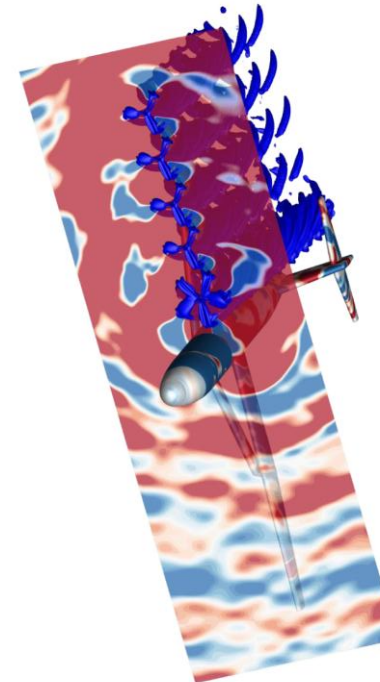
## ■ SM

- IMMIS+ provided by partner DLR for noise assessment
- EPNL (effective perceived noise level) as function of the propeller **diameters**, **tip Mach** number and **Thrust** (different for the IB and OB propellers)



## Experimental activity

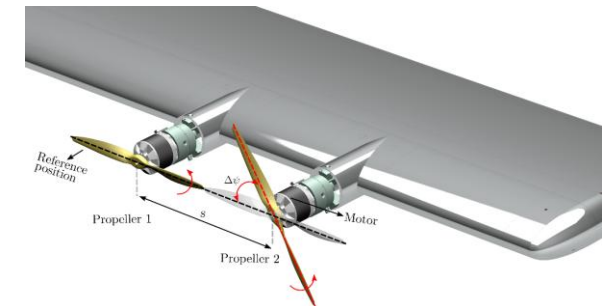
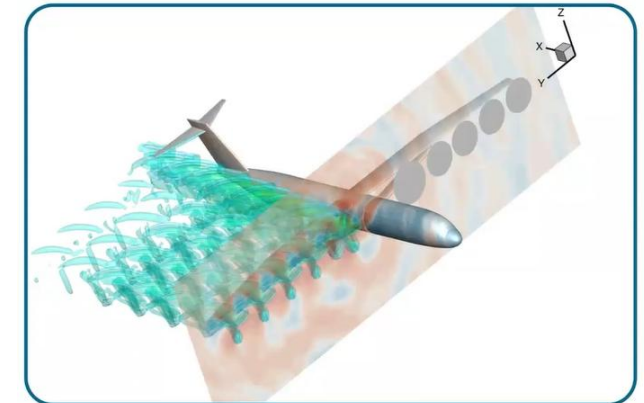
- Propeller-wing
- Propeller-propeller
- Phase shifting
- Used to calibrate the CAA solvers



## High-fi

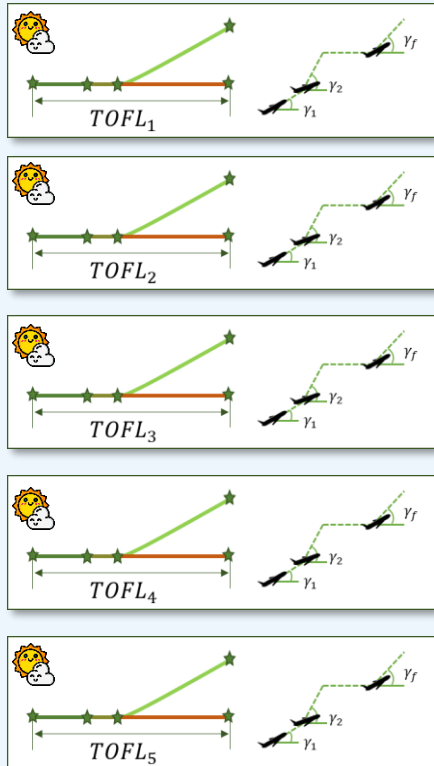
## CAA

- Multifidelity
- CFD
- LBM
- **Calibrated on wind tunnel**
- Used on post MDO for fine-tuning
- Used for impact assessment

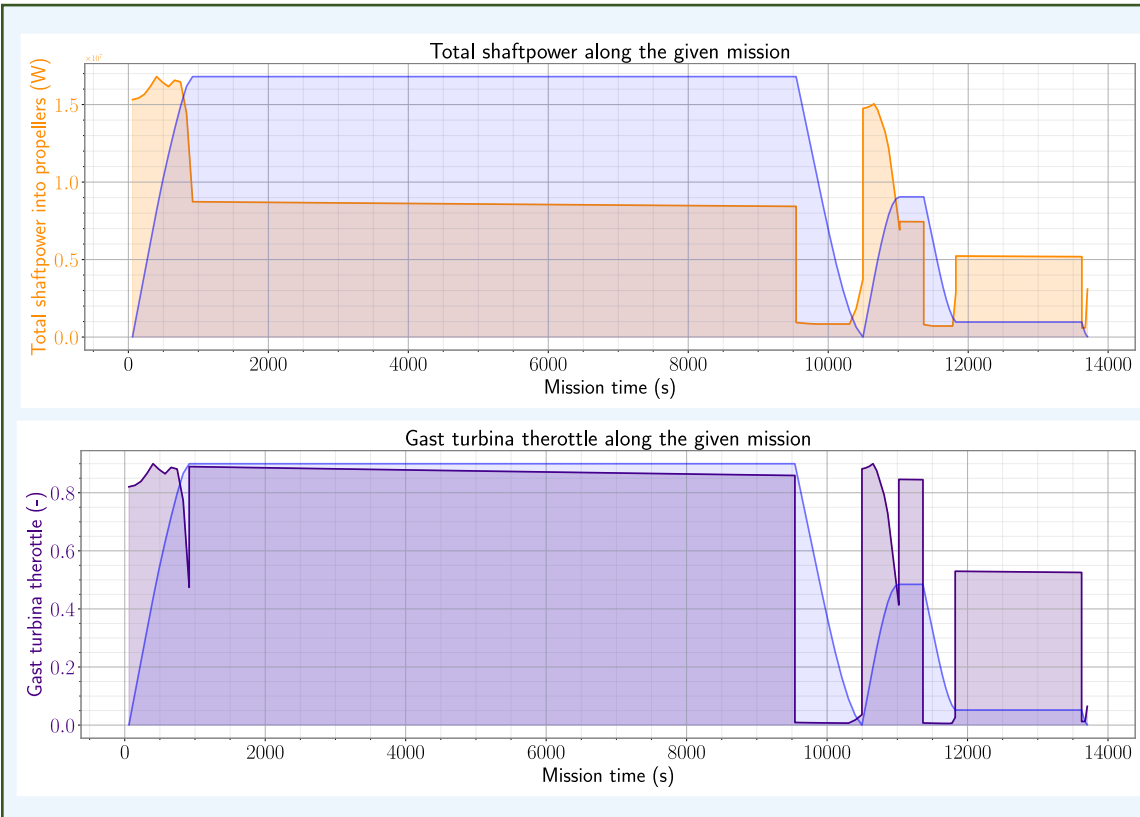


- Mission (Nominal + Diversion)
- TOFL and RLD Evaluation (wet/dry, failure conditions, inspired by FAR/CS25)
- Climb Gradients (failure conditions, inspired by FAR/CS25)

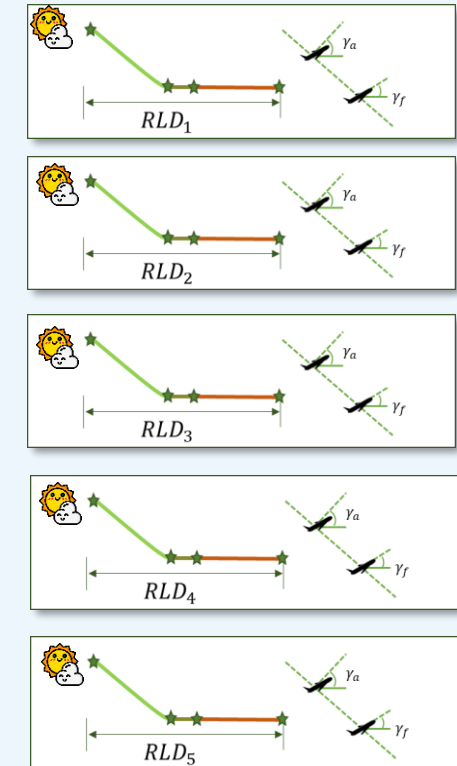
### Takeoff and climb segments



### Main and extended certification mission



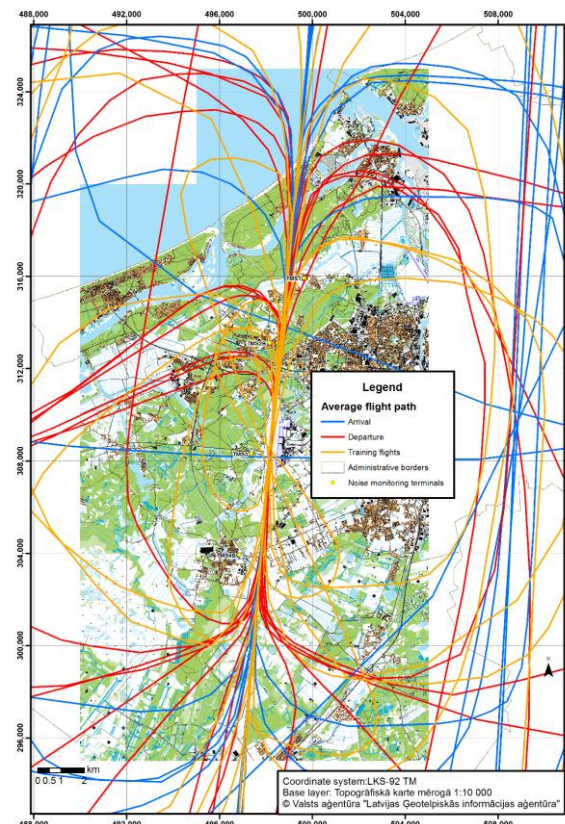
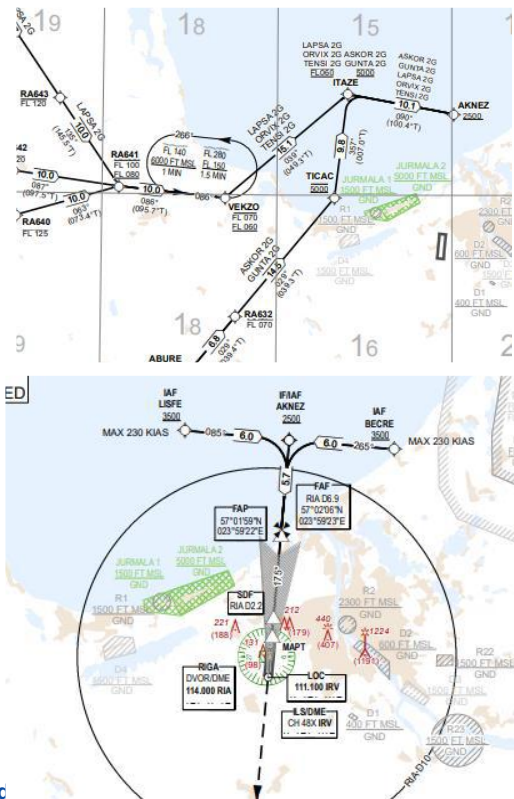
### Approach and landing segments





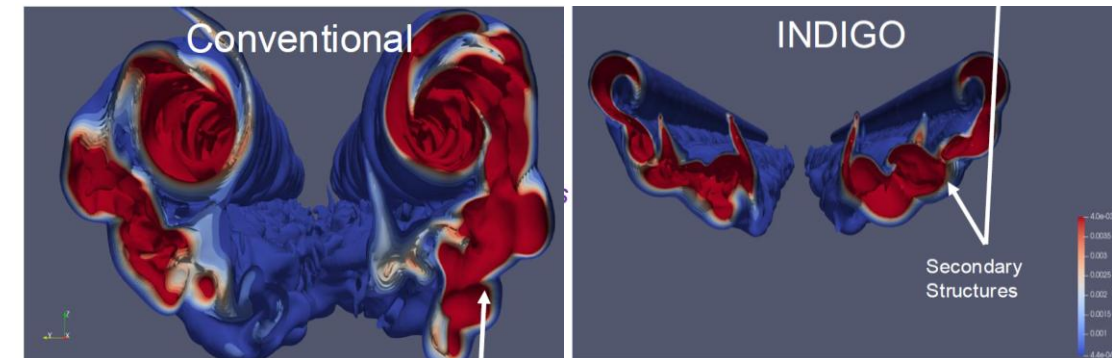
## Airport trajectories

- RIGA, Madrid, Barcelona, Dortmund
- Trajectories
  - Most flown
  - Better/Worst
    - LAQ
    - Noise

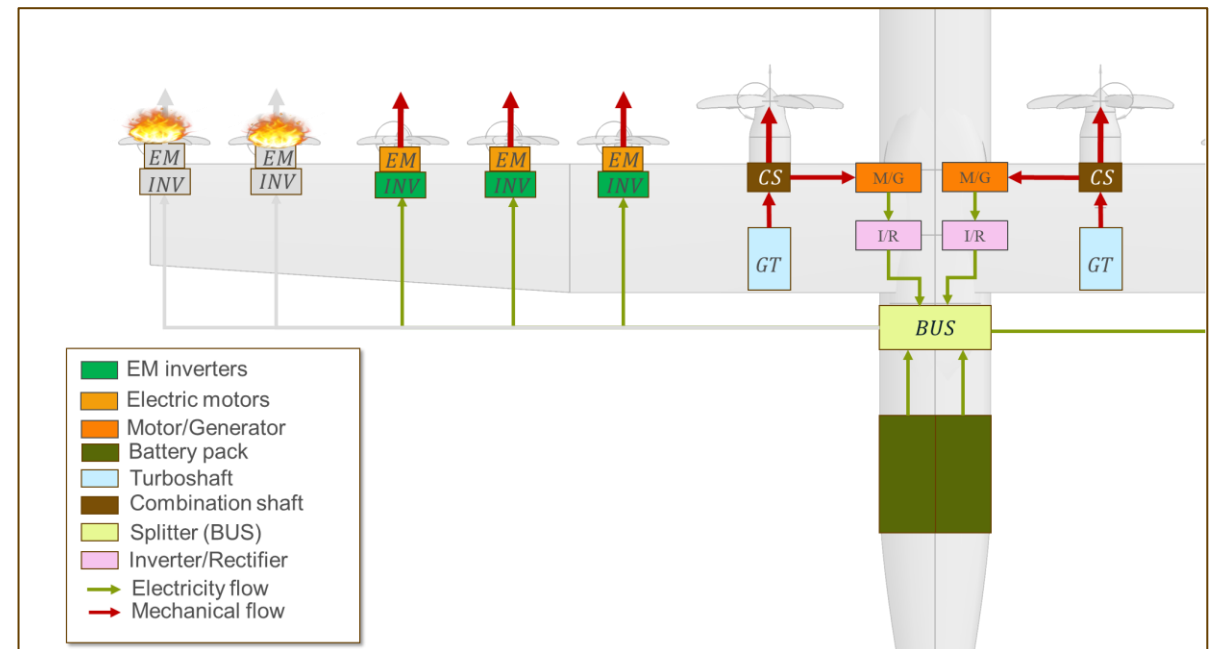
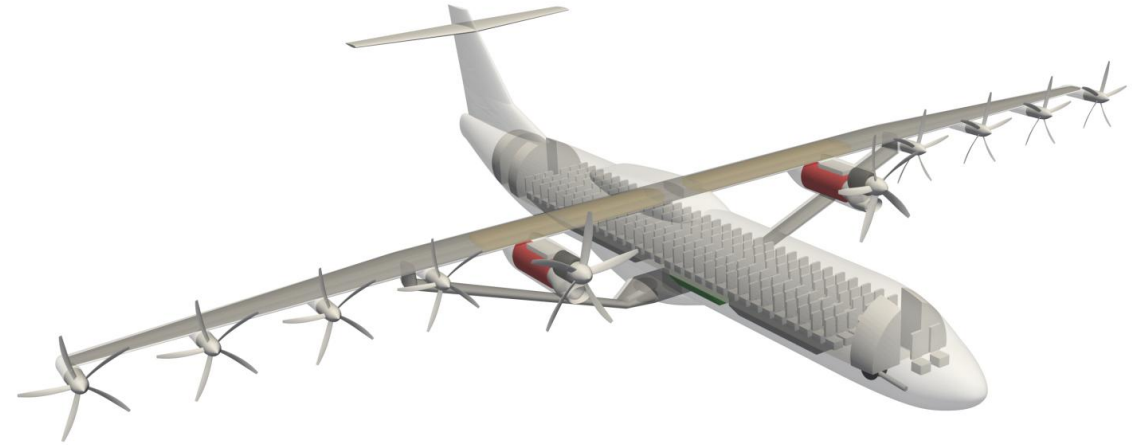


## Pollutant Dispersion

- LES modelling of vortices dynamics
- Assessment of pollutant concentration in populated areas
- Calibration of available methods on INDIGO's aircraft
- **Used after MDO**



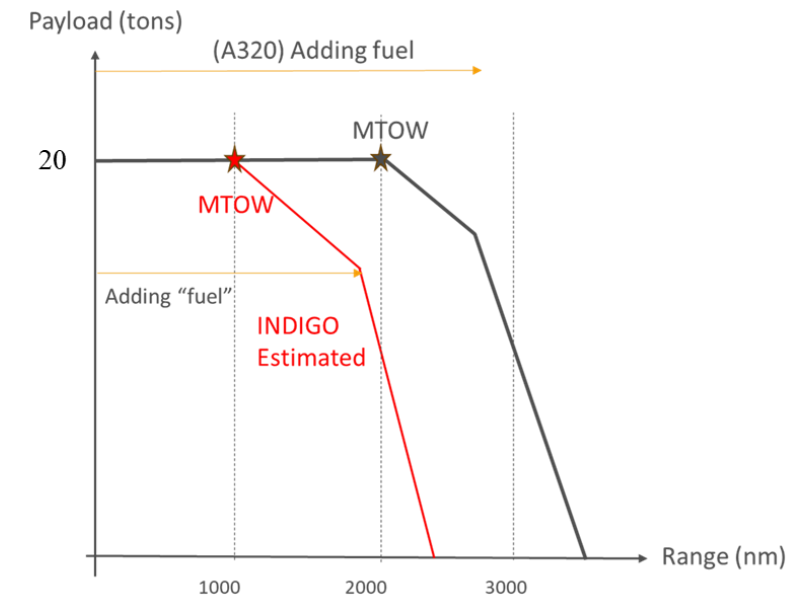
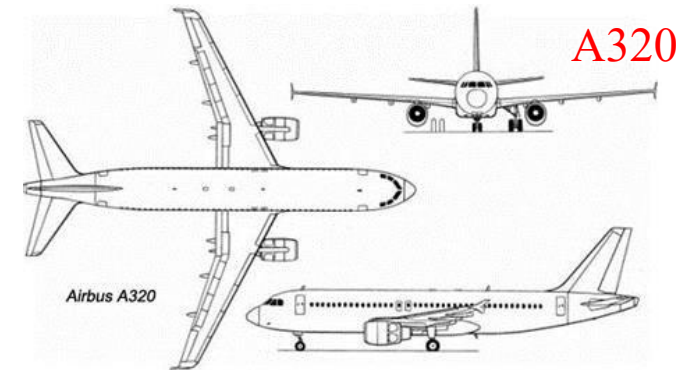
- Introduction
- Methodology
- **Optimization campaign**





## Reference vs Indigo Aircraft

	INDIGO	A320
MTOW	79 t	79 t
MPW	20 t	20 t
Wing Area	122.6 m <sup>2</sup>	122.6 m <sup>2</sup>
Range @ Max Payload	1000 nm	~2000-2500 nm
Cruise altitude	6000 m	~ 11000 m
Mach @ cruise	0.6	0.78



## Optimization problem

$$\begin{cases} \min_x \text{obj}(x) \\ \text{subject to } g(x) \leq 0 \\ h(x) = 0. \end{cases}$$

$$\text{obj} = F^* + \alpha \cdot G^* + \beta \cdot N^*$$

$F^*$ : Non-dimensional block fuel along the **nominal mission**  
 $G^*$ : Non-dimensional fuel burn **below 900m**  
 $N^*$ : Non-dimensional **noise measure**

Viability  
(block fuel)

LAQN metrics (operations below 900)

- **Gaseous part**
  - Integration of fuel burn
  - NOx, CO2 and other derivatives can be evaluated as byproduct
- **Noise Part**
  - EPNL

$\alpha$  → relevance of **fuel burn below 900m**  
(indicators of Gaseous Emissions)

$\beta$  → relevance of **noise**  
(indicators of emitted Noise)

Optimization algorithm:  
SNOPT

## Optimization problem

$$\begin{cases} \min_{x} obj(x) \\ \text{subject to } g(x) \leq 0 \\ h(x) = 0. \end{cases}$$

### Airframe

- Wing planform DVs
- Other wing and strut outer-mold line DVs (but airfoils class is fixed)

### Powertrain

- Max **power of electric** and **thermal** components
- Propeller design, **Diameter** and  $M_{tip}$  (RPMs as consequence) and **solidity** of the blade.
- Hybridization factors **HF** along mission segments
- Relative propeller power/thrust  $\psi$  along mission segments

Design variable	Units	Lower	Upper	Design variable	Units	Lower	Upper
<b>Wing Planform</b>							
AR	-	15	25	Taper ratio	-	0.31	0.33
Twist @ wing root	deg	-3	3	Twist @ wing tip	deg	-5	1
Twist @ strut	deg	-3	3	Strut chord	-	0.906	1.597
t/c @ root	-	12%	18%	t/c @ tip	-	9%	14%
<b>Powerplant components</b>							
Turboshaft	hp	3000	40000	Electric motor	hp	500	40000
Combination gearbox	hp	1000	100000	Inverter	hp	500	10000
Inverter/rectifier/generator assembly	hp	500	40000	Battery Weight	kg	10	100000
<b>Propellers</b>							
Propeller IB diameter	m	1.5	5	Propeller OB diameter	m	1.5	5
Propeller IB TipM	-	0.5	0.78	Propeller OB TipM	-	0.5	0.78
Propeller IB solid_factor	-	0	1	Propeller OB solid_factor	-	0	1
<b>Ground and flight phases</b>							
HF (initial)	-	-20	1	HF (final)	-	-20	1
psi (initial)	-	0.2	10	psi (final)	-	0.2	10

Total:  
**186 DVs**

## Optimization problem

$$\begin{cases} \min_x obj(x) \\ \text{subject to } g(x) \leq 0 \\ h(x) = 0. \end{cases}$$

Total:

**~5500 constraints**

### Performance and Airworthiness

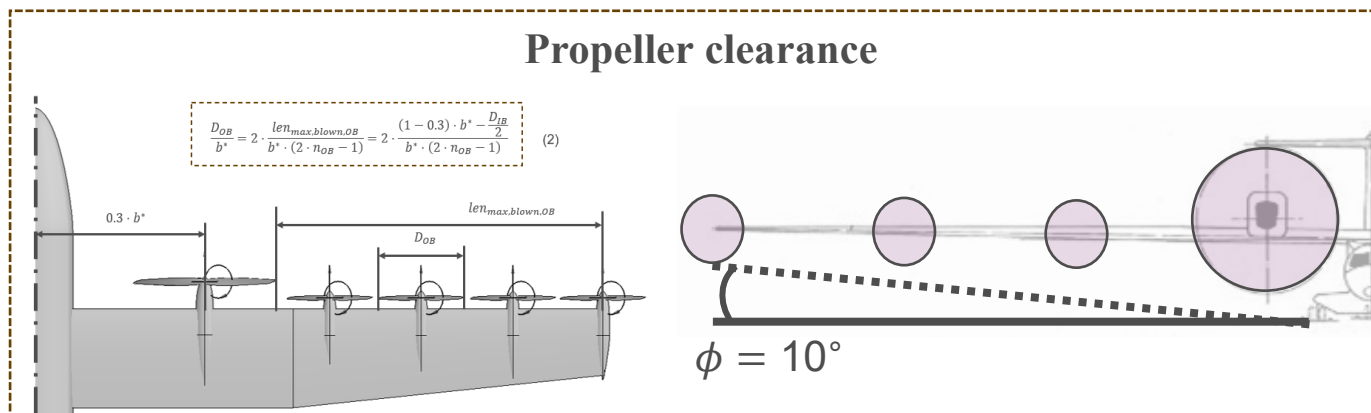
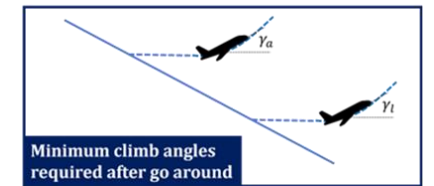
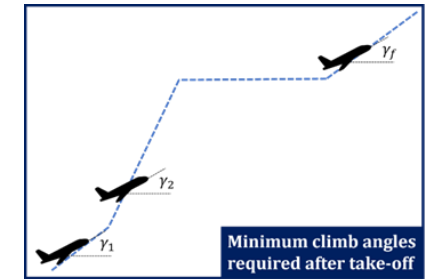
- TOFL < target TOFL (2190 m)
- LFL < target LFL
- Climb gradients
- Yawing constraints (failure case 2)
- $C_p \leq 1.2$  (far from stall)

### Geometric

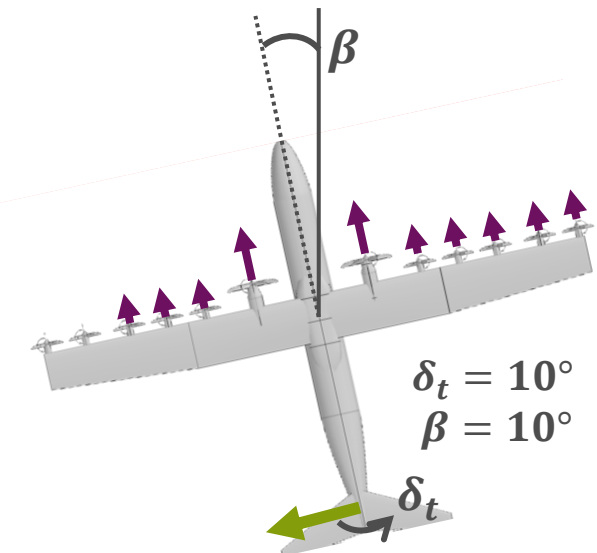
- Gap between propellers (non-overlapping)
- Clearance during roll maneuver

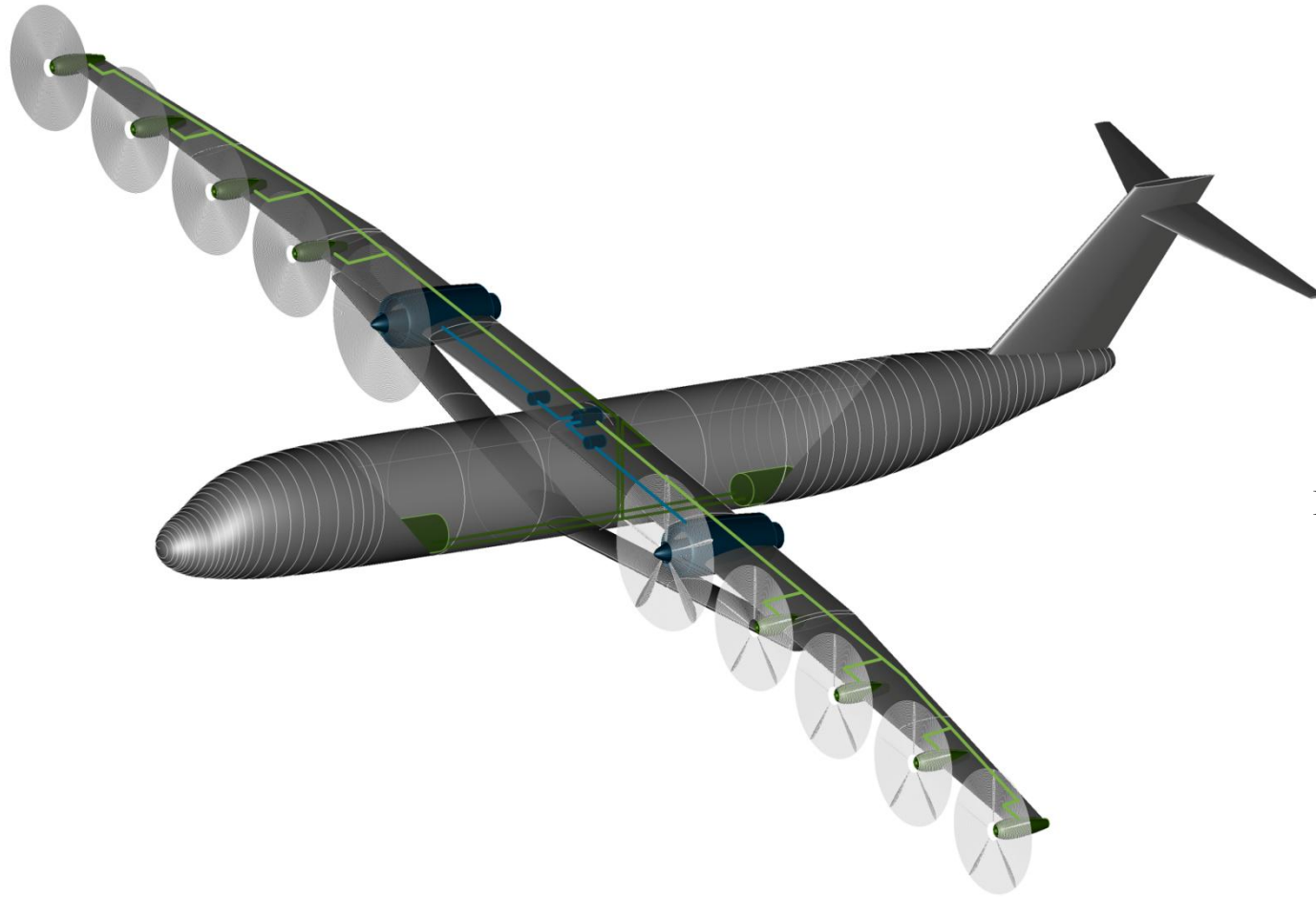
### MDA Feasibility

- Power < Power Rating (for all components)
- SoC of battery > 0.2 (can recharge!)

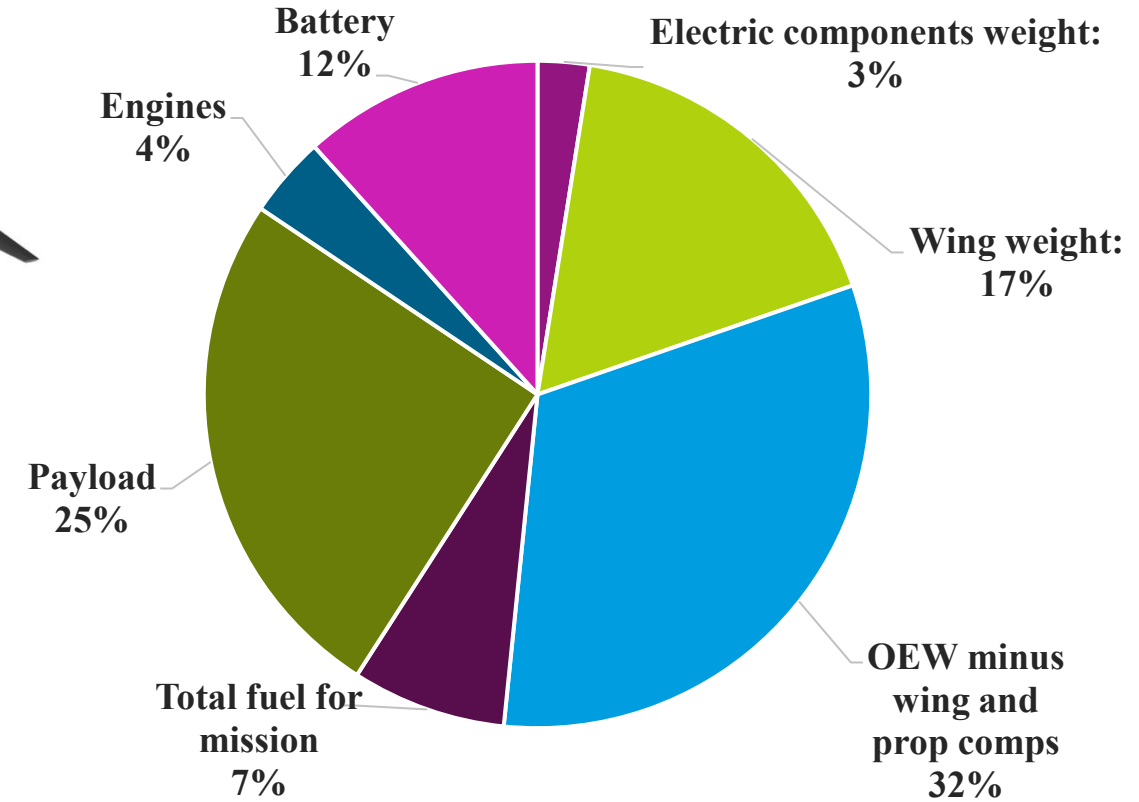


### Yawing constraint during FC2:





Weight breakdown - 10SPH



Variable	units	Value	Variable	units	Value
Propeller IB diameter	m	5	Comb gearbox weight	kg	103.4
Propeller OB diameter	m	4.0	Dimensional Aspect ratio	None	21.6
Propeller IB mach number	None	0.6	Dimensional Taper ratio	None	0.4
Propeller OB mach number	None	0.6	Dimensional Wing root twist	deg	-3.0
Propeller IB solid fraction	None	0.7	Dimensional Wing tip twist	deg	-5.0
Propeller OB solid fraction	None	0.3	Dimensional Strut twist	deg	1.6
Inverter rating	MW	1.7	Dimensional Strut chord	m	1.6
Inverter rectifier rating	MW	1.8	Dimensional Root thickness	None	0.2
<b>Engine rating</b>	MW	<b>6.7</b>	Dimensional Tip thickness	None	0.1
<b>Electric motor rating</b>	MW	<b>1.6</b>	Trip fuel	kg	4530.4
Gearbox rating	MW	2.0	Total fuel	kg	5912.4
<b>Battery weight</b>	kg	<b>9215.8</b>	OEW	kg	43871.7
Inverter weight	kg	94.1	<b>Wing weight</b>	kg	<b>13577.7</b>
Inverter rectifier motor weight	kg	196.0	Mean EPNL	None	74.9
Engine weight	kg	1547.6	Fuel burnt below 900m	kg	72.4
Motor weight	kg	79.2			

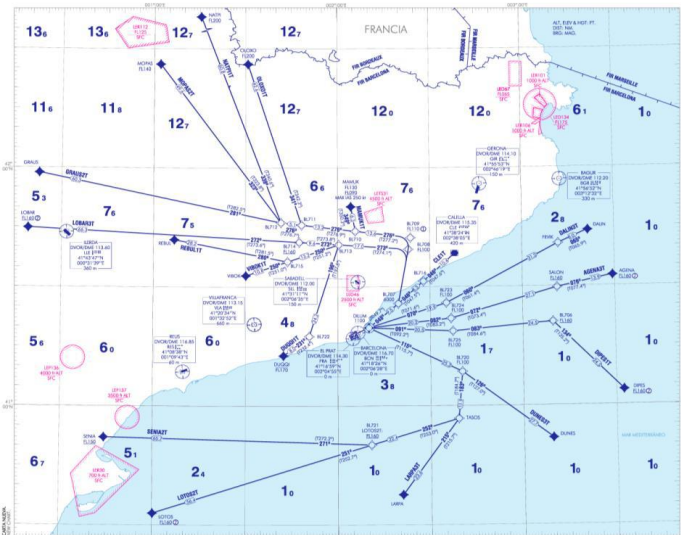
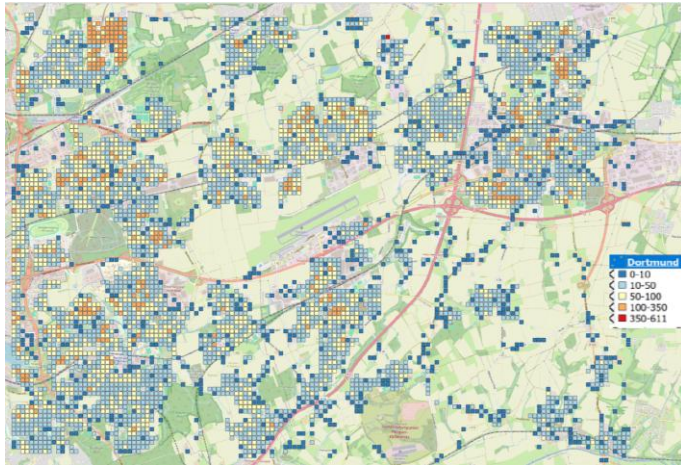
## Comparison with A320

- Same Payload (specific pollution)
- Same Mission Range

	INDIGO	A320	Improv %
<b>Block fuel [kg]</b>	4530.5	6479.7	30.1
<b>Fuel burn &lt; 900m [kg]</b>	72.4	227.6	68.2
<b>Noise (avg TO EPNL) [dB]</b>	77.5	83.5	6.0 dB



$$obj = F^* + \boxed{\alpha \cdot G^* + \beta \cdot N^*}$$



## LAQN metrics (operations below 900)

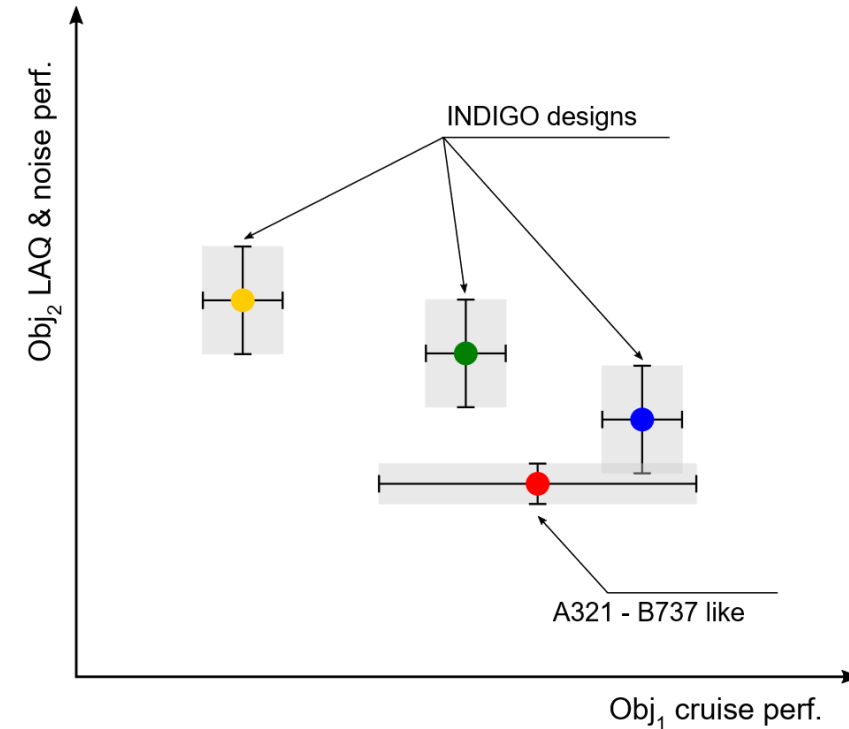
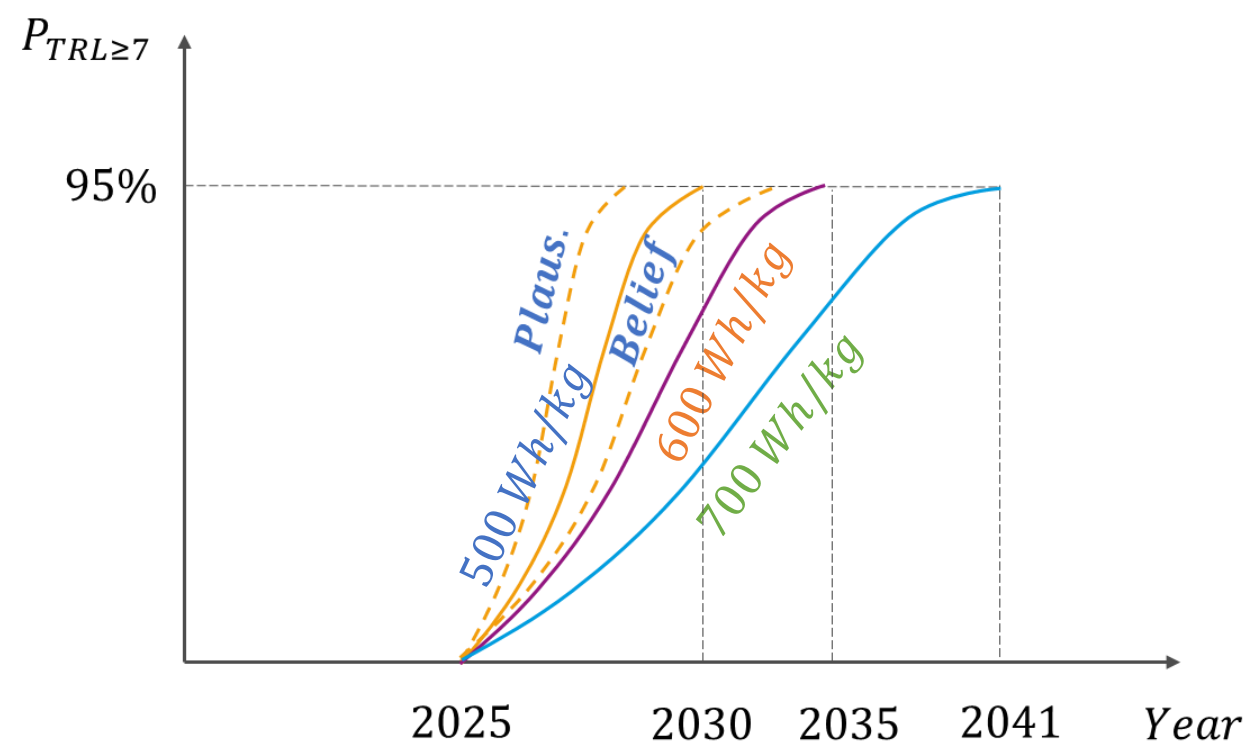
- Gaseous and Noise concentrations measures (weighted by population density)
- Surrogate model
- **Gaseous part**
  - AeroMOD (emitted → air dispersion → concentration)
  - NO<sub>x</sub>, CO<sub>2</sub> and other derivatives weighted by health impact
- **Noise Part**
  - EPNL in populated regions!

## Multi-missions

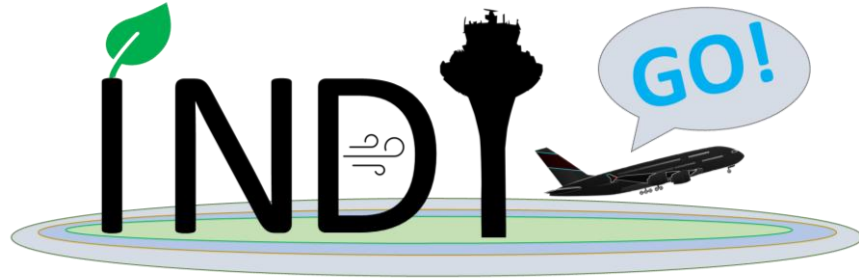
- 20 TO trajectories
- 20 LA trajectories

## Uncertainties

- On batteries technological level (energy/power density)



Dempster-Shafer evidence theory to determine optimistic (plausibility) and pessimistic margins of a given required battery feature.



**Website:** <https://indigo-sustainableaviation.eu/>

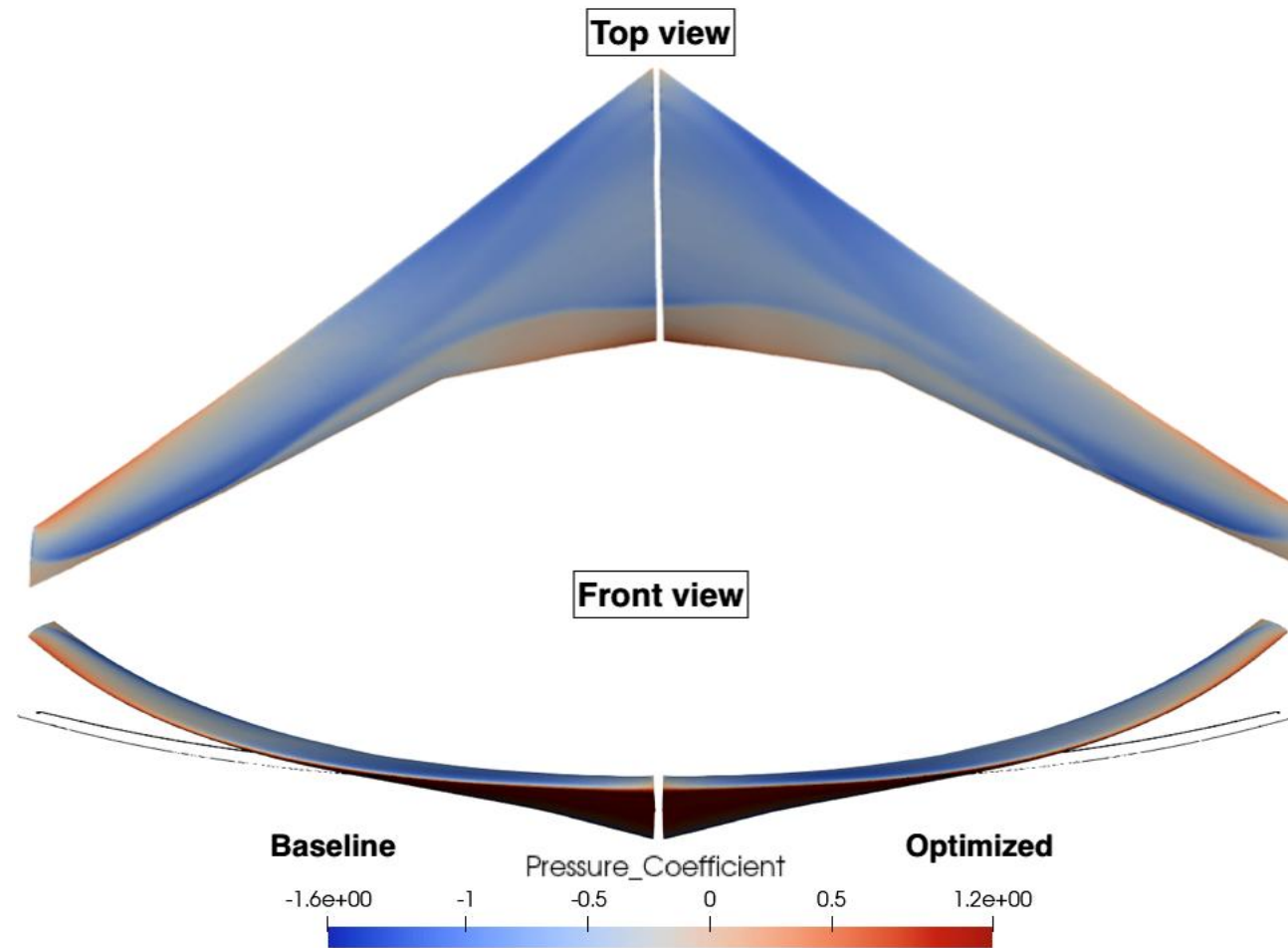
**LinkedIn:** [linkedin.com/company/ indigo-he-project/](https://www.linkedin.com/company/indigo-he-project/)

The activities described in this paper have been carried out under the project **INDIGO** (Integration and Digital Demonstration of Low-emission Aircraft Technologies and Airport Operations), coordinated by **Universidad Carlos III de Madrid**.



INDIGO project has received fundg from the European Climate, Infrastructure and Environment Executive Agency (CINEA) under the Horizon Europe programme under grant agreement No 101096055. in





- New **generation** of aircraft → more **efficient** design:
  - **Unconventional** configurations with large AR, and/or
  - **Lighter** and more **flexible** aircraft structures.
- Expected **significant** wing **deflections** while in operation: strong **aeroelastic** (aero-structural) **coupling**.
- Required adequate **analysis** approaches.
- High-fidelity earlier to reduce time-to-market and/or risks.
- Not only analysis but design and (coupled) **optimization**



A350 ultimate load wing deflection



Cruise and ultimate load wing deflections of the B787

10% semi-span wing tip deflection in flight.



## High-fidelity aerostructural optimization. How?

- Employ **high-fidelity** solvers into coupled **aerostructural optimization** processes:
  - **Larger cost** per evaluation of aeroelastic solutions.
  - **High-sensitivity** with respect to **small geometric features** → **higher number** of Design Variables (**DVs**) needed to exploit potential of high-fidelity optimization.
- Influence on the optimization approach:
  - Gradient-based optimization is an appealing choice
  - **Adjoint method** makes gradient calculation almost **independent** on the number of **DVs** (as opposed to other strategies)
- Highly **modular**: each discipline solver is self-contained and communicates at high level by means of an orchestrator.



**Adjoint  
method**



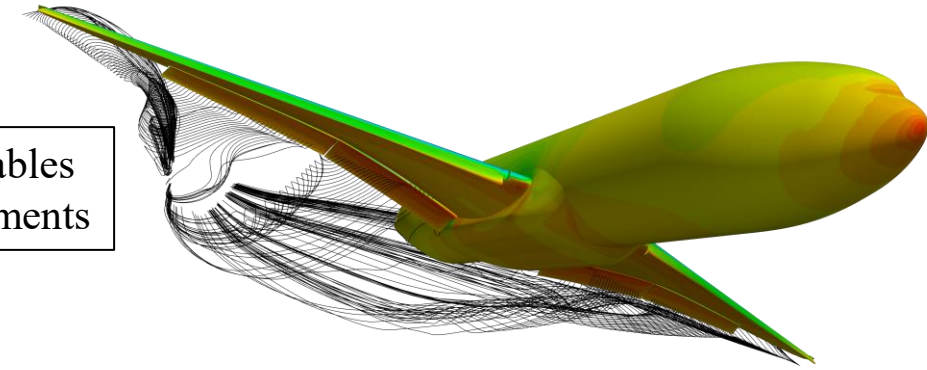
## CFD solver (SU2)

- Flow models: **Euler**, **RANS**, etc.
- **(Arbitrary Lagrange Euler) ALE** formulation.

$$\mathcal{F}(\mathbf{w}, \mathbf{z}) = \frac{\partial \mathbf{w}}{\partial t} + \nabla \cdot \mathbf{F}^c(\mathbf{w}, \mathbf{z}) - \nabla \cdot \mathbf{F}^v(\mathbf{w}, \mathbf{z}) - \mathbf{Q}(\mathbf{w}, \mathbf{z}) = 0$$

$\mathbf{w} \rightarrow$  flow conservative variables  
 $\mathbf{z} \rightarrow$  volume mesh displacements

**SU2**  
code



## Fluid mesh deformation solver (SU2)

- **Linear** (pseudo-)elastic volume deformation method.

$$\mathcal{M}(\mathbf{z}, \mathbf{u}_f) = \mathbf{K}_m \cdot \mathbf{z} - \tilde{\mathbf{f}}(\mathbf{u}_f) = 0$$

$\mathbf{u}_f \rightarrow$  displacements at the surface

### Implementation

- C++ core.
- Top level functions wrapped in Python.
- Handling **AD** by means of **CoDiPack** library.
- Hybrid MPI-MP parallelization

- ADL, Stanford University
- P&P, TU Delft
- SciComp, TU Kaiserslautern
- CREA Lab, Politecnico di Milano
- Imperial College London MTFC Group,
- University of Liege
- van der Weide Group, U. of Twente
- New Concepts in Aeronautics Lab, ITA
- Strathclyde University
- Robert Bosch LLC
- ECN part of TNO
- [Universidad Carlos III de Madrid \(UC3M\)](#)

## In-house Structural FE solver (pyAUGUSTO)

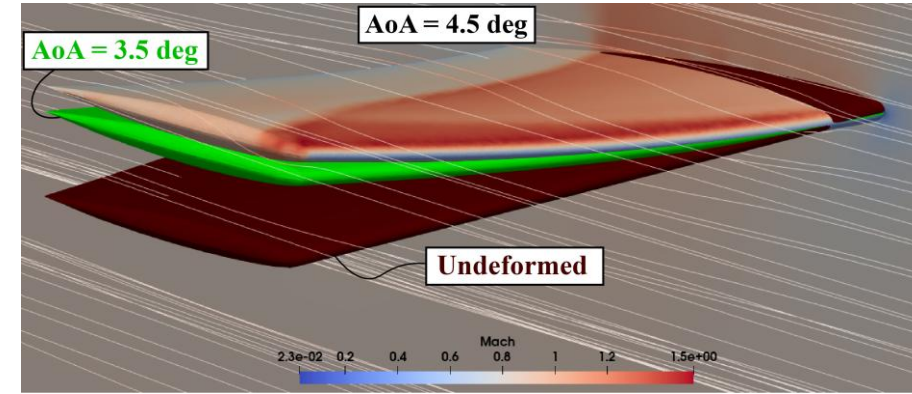
- Shells (Plate & membranes), beams, nonlinear rigid elements
- Geometric **nonlinearities** (large displacements)

$$S(\mathbf{u}_s) = \mathbf{f}_s - \mathbf{f}_{int}(\mathbf{u}_s) = \mathbf{0}$$

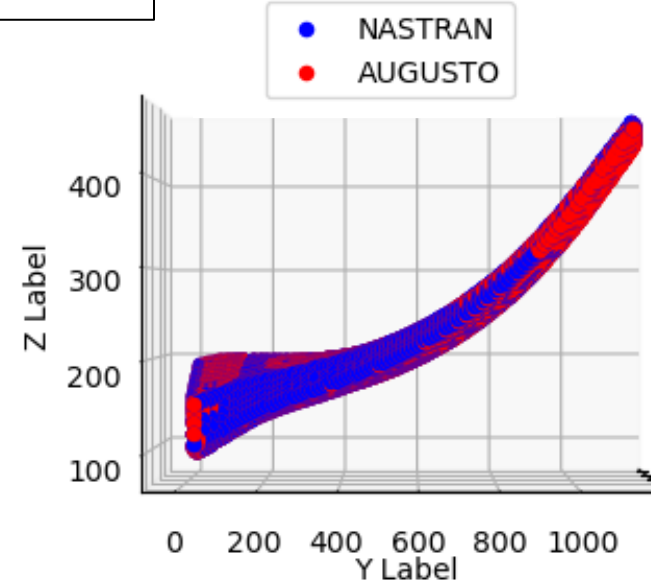
$\mathbf{u}_s \rightarrow$  structural displacements variables  
 $\mathbf{f}_s \rightarrow$  applied forces

## Implementation

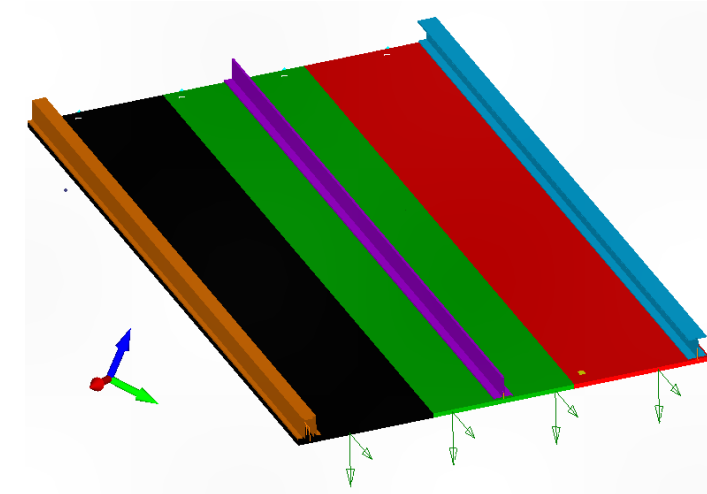
- C++ core.
- Top level functions wrapped in Python.
- Developed to handle **AD** by means of **CoDiPack** library.
- MPI parallelism



ONERA M6 test case at aeroelastic equilibrium with different AoAs.



Very flexible NASA CRM deflection



Stiffened panel

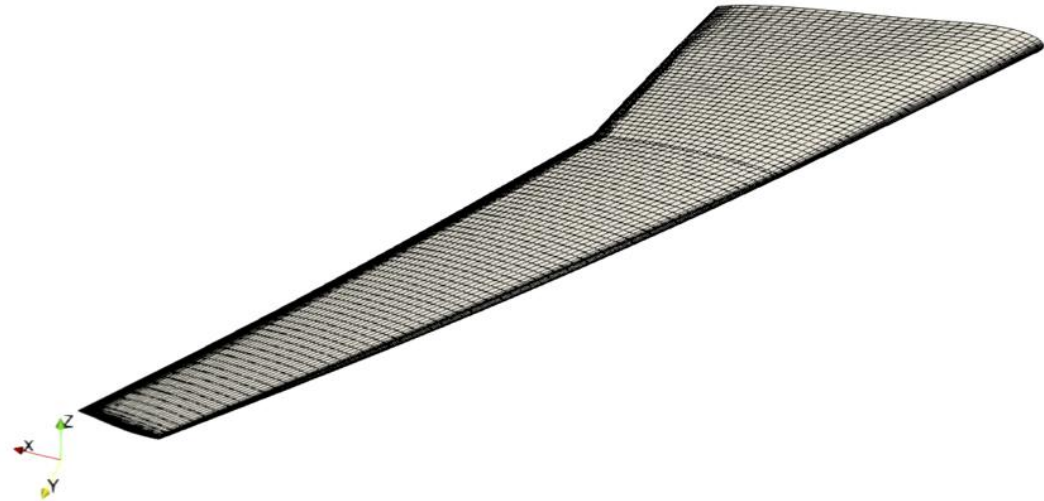
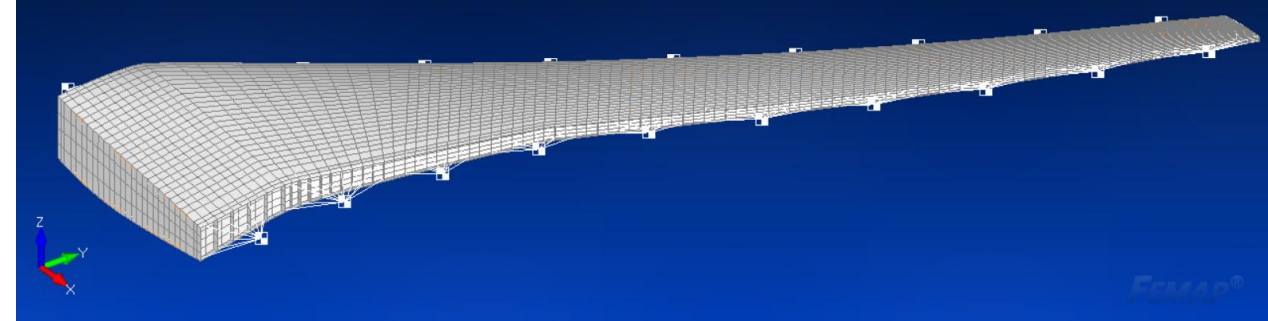
## Interfacing method (MLS)

- Transfer information between non-conformal grids\*.
- Based on **Radial Basis Functions**.

$$\begin{cases} \mathbf{u}_f = \mathbf{H}_{MLS} \mathbf{u}_s \\ \mathbf{f}_s = \mathbf{H}_{MLS}^T \mathbf{f}_f \end{cases}$$

## Implementation

- C++ core.
- Top level functions wrapped in **Python**.
- **Ad-hoc** developed.



\*Quaranta G, et al (2005) A conservative mesh-free approach for fluid structure problems in coupled problems. In: International conference for coupled problems in science and engineering, Santorini, Greece. pp 24–27

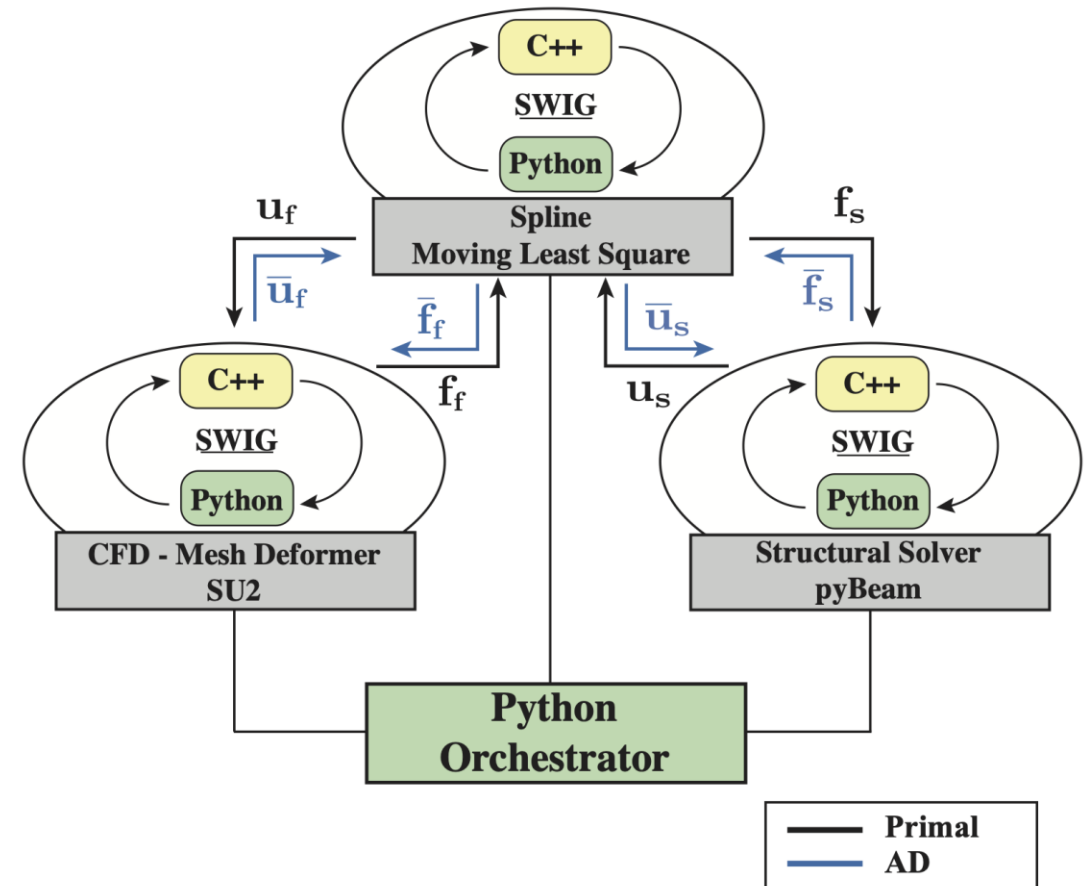
## Coupling method (Orchestrator)

- **3-field** formulation.
- **Block Gauss-Seidel** (BGS) iterative solution strategy.
- **Relaxation** of displacements to ensure convergence.
- Primal and dual.

$$\mathcal{G}(\mathbf{u}_s, \mathbf{w}, \mathbf{z}) = \begin{cases} \mathcal{S}(\mathbf{u}_s, \mathbf{w}, \mathbf{z}) = 0, \\ \mathcal{F}(\mathbf{w}, \mathbf{z}) = 0, \\ \mathcal{M}(\mathbf{u}_s, \mathbf{z}) = 0, \end{cases}$$

## Implementation

- **Python** coded.
- Wraps solvers (primal/dual problems).
- Interfaces with **optimizer**.
- **Ad-hoc** developed.



Application: wing-shape aerostructural optimization (2021)

- **Response (objective/constraints)**
  - **Fluid:** drag coefficient
- **DVs:**
  - **Geometric** (variation of wing jig shape)

$$\min_{u_{F\alpha}} \quad J = C_D(w, z)$$

subject to

$$\begin{aligned} F(w, z) - w &= 0 \\ F_f(w, z) - f_f &= 0 \\ M(u_{tot}) - z &= 0 \end{aligned}$$

$$H^T f_f - f_s = 0$$

$$S(u_s, f_s) - u_s = 0$$

$$H u_s - u_f = 0$$

$$u_{tot} - u_f - u_{F\alpha} = 0$$

Fluid solver

Force calculation (on the wing surface)

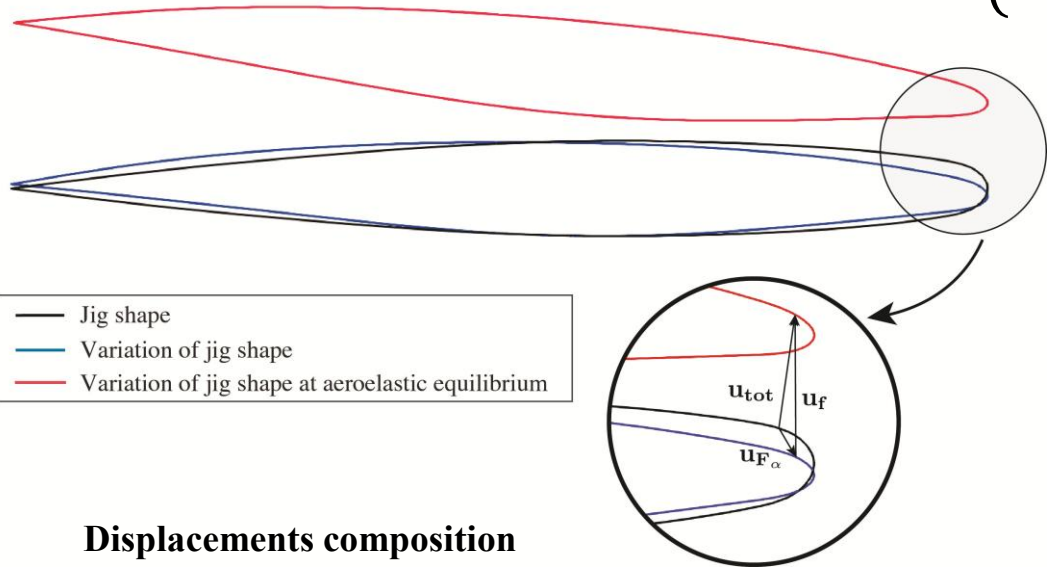
Mesh deform. solver

Force transfer

Struct. solver

Struct. disp. transfer

Displacement composition



State variables	
$u_s$	Structural displacements
$w$	Flow conservative variables
$z$	Volume mesh displacements
$f_f$	Fluid loads
$f_s$	Structural loads
$u_f$	Displacements of wing surface due to deflection
$u_{tot}$	Cumulative displacements of wing surface

## Adjoint equations and objective gradient

$$\bar{w}^T = \frac{\partial J}{\partial w} + \bar{w}^T \frac{\partial F}{\partial w} + \bar{f}_f^T \frac{\partial F_f}{\partial w}$$

$$\frac{\partial J}{\partial f_f} - \bar{f}_f^T + \bar{f}_s^T H^T = 0$$

$$\frac{\partial J}{\partial z} + \bar{w}^T \frac{\partial F}{\partial z} + \bar{f}_f^T \frac{\partial F_f}{\partial z} + \bar{z}^T = 0$$

$$\frac{\partial J}{\partial f_s} - \bar{f}_s^T + \bar{u}_s^T \frac{\partial S}{\partial f_s} = 0$$

$$\bar{u}_s^T = \frac{\partial J}{\partial u_s} + \bar{u}_s^T \frac{\partial S}{\partial u_s} + \bar{u}_f^T H$$

$$\frac{\partial J}{\partial u_f} - \bar{u}_f^T - \bar{u}_{tot}^T = 0$$

$$\frac{\partial J}{\partial u_{tot}} + \bar{z}^T \frac{\partial M}{\partial u_{tot}} + \bar{u}_{tot}^T = 0$$

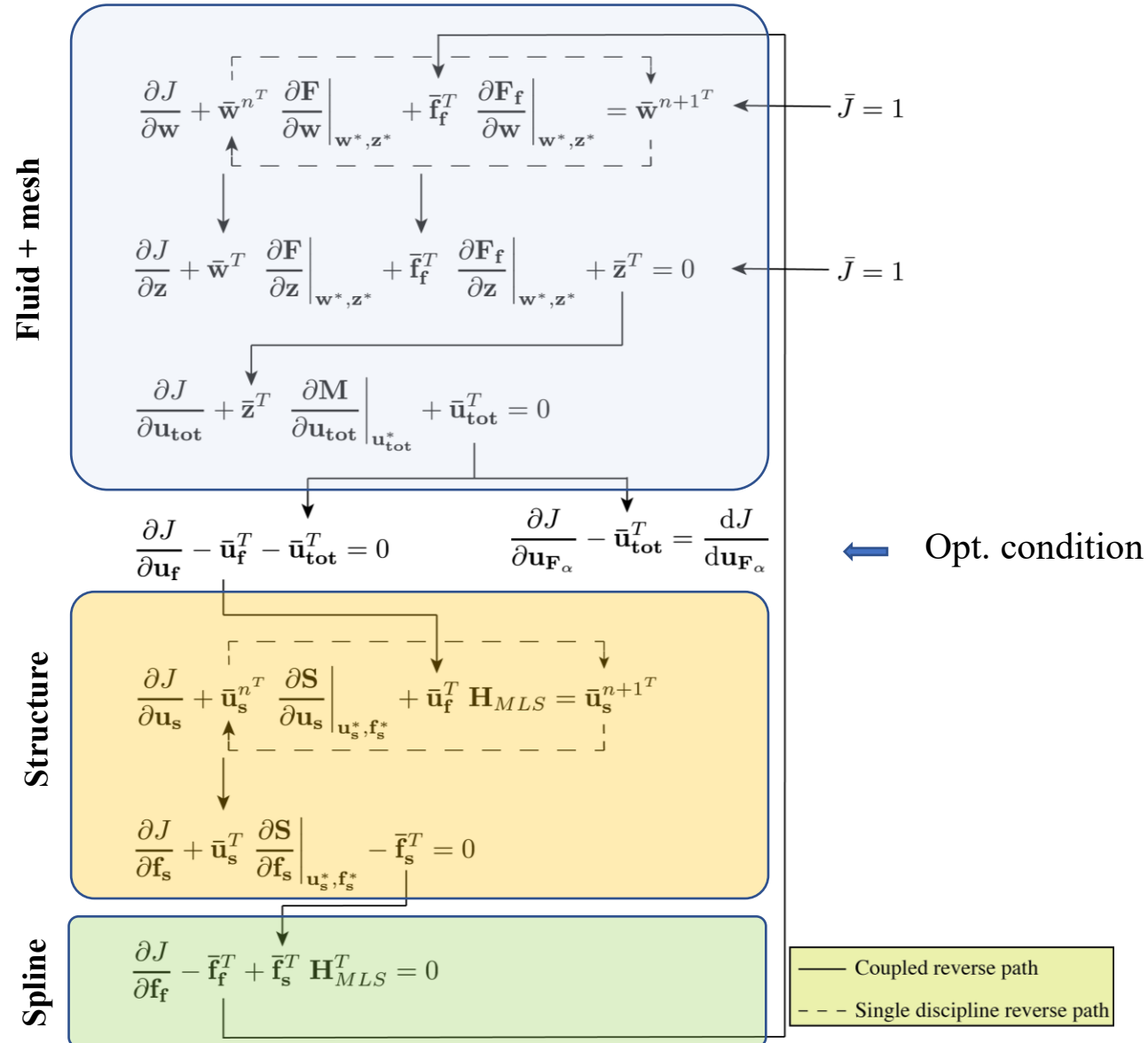
$$\frac{dJ}{du_{F\alpha}} = \frac{\partial \mathcal{L}}{\partial u_{F\alpha}} = \frac{\partial J}{\partial u_{F\alpha}} - \bar{u}_{tot}^T$$

## How to solve this system of equations?

- Main blocks are
  - CFD and mesh solvers, coupled within **SU2**
  - CSD solver
  - Interface module
- A monolithic solution is not efficient (different physics are better treated by dedicated solvers), not convenient/viable (memory to store the computational graph)
- Ideally, different solvers treat a block of these equations.
- Coupling due to dependency of adjoint equation of one solver to adjoint variables calculated in other solvers



## Adjoint and objective gradient



Iterative solution:

- At the **discipline solver level** (nonlinear primal solver in FP).
- At the **interdiscipline level** (source term exchanged through orchestrator).

### State variables

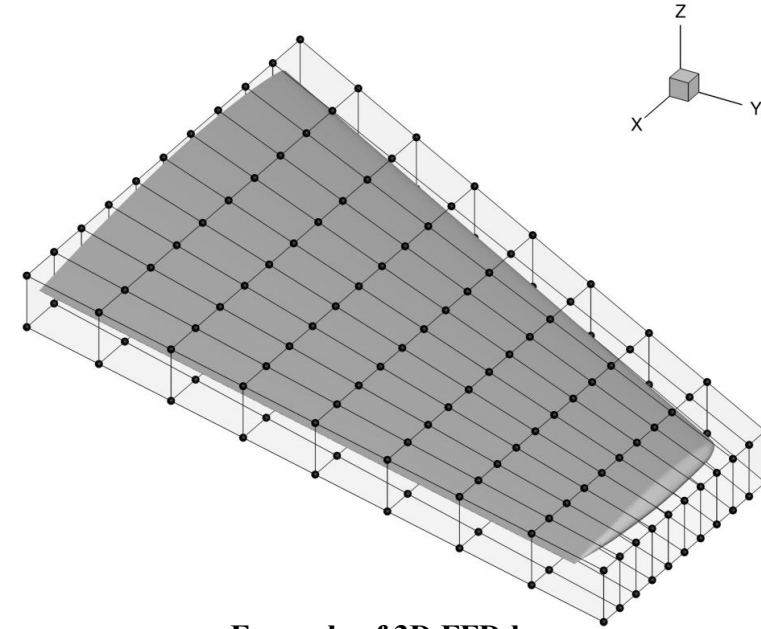
$\mathbf{u}_s$	Structural displacements
$\mathbf{w}$	Flow conservative variables
$\mathbf{z}$	Volume mesh displacements
$\mathbf{f}_f$	Fluid loads
$\mathbf{f}_s$	Structural loads
$\mathbf{u}_f$	Displacements of wing surface due to deflection
$\mathbf{u}_{\text{tot}}$	Cumulative displacements of wing surface

With minimum effort on the workflow it is possible to:

- Select **different responses (objective function/constraint)**
- Add different **DVs**.

## Aerostructural wing shape optimization

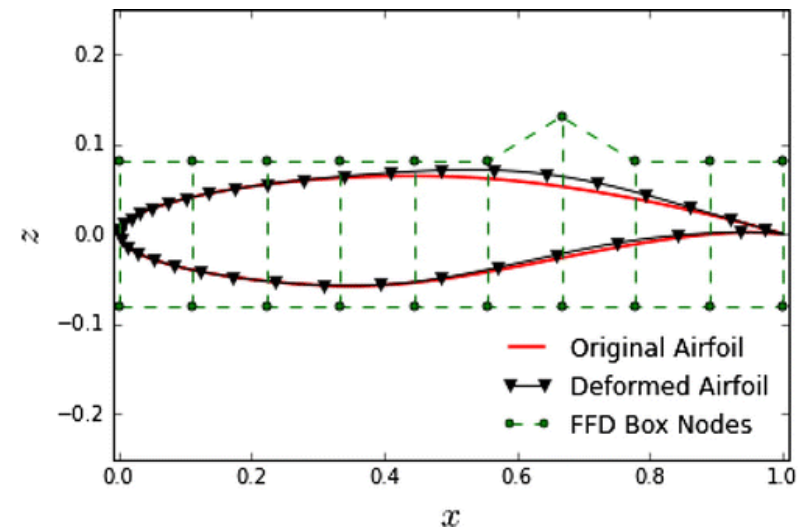
- Algorithm: Sequential Least Square Quadratic Programming (SLSQP).
- **Free Form Deformation** (FFD) technique.
- **FFD box** discretized with given number of **Control Points** (CP), which are the DVs given to optimizer.



Example of 3D FFD box

## Constraints

- Geometric constraints (e.g., t/c) and their gradients evaluated by SU2 module **SU2\_GEO**.
- Prescribed  $C_L$  accommodated internally by SU2 (not treated at optimization level).



2D FFD technique on airfoil\*

## Importance of considering aerostructural coupling

Two optimization strategies:

- Aerodynamic Wing Shape Optimization (**AWSO**).
  - **Rigid** configuration.
  - **No aerostructural coupling** in primal/dual problems.
- **Aerostructural** Wing Shape Optimization (**ASWSO**).
  - Configuration at aeroelastic equilibrium: **flying shape**.
  - **Aerostructural coupling** in primal/dual problem.
  - **Intermediate approach**: aerostructural coupling in the primal problem only

**AWSO** optimum is, compared, at **aeroelastic equilibrium**, to the **ASWSO** optimum.

## Asymptotic flow conditions

- $C_L = 0.5$ ;  $M_\infty = 0.85$ .

## Optimization of the CRM

### Aerodynamic constraints

$$C_L = 0.5$$

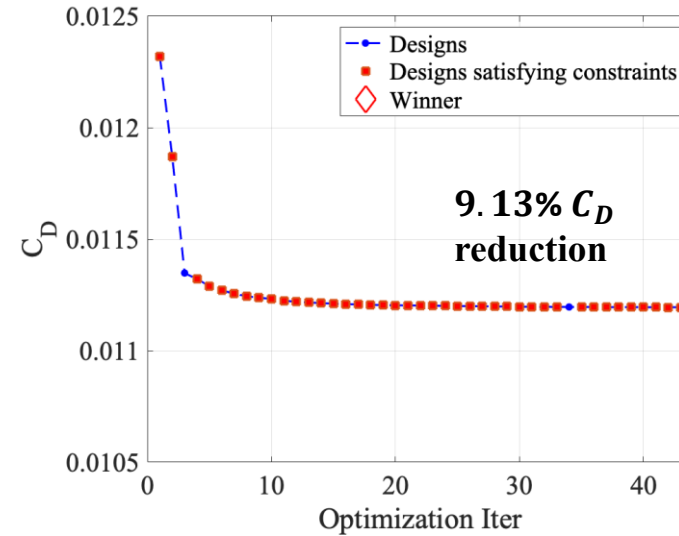
### Geometric constraints

t/c (sec. at 0.34% span)	$\geq$	15.6%
t/c (sec. at 16.32% span)	$\geq$	12.5%
t/c (sec. at 27.01% span)	$\geq$	11.2%
t/c (sec. at 38.49% span)	$\geq$	10.4%
t/c (sec. at 49.76% span)	$\geq$	10.0%
t/c (sec. at 60.74% span)	$\geq$	9.8%
t/c (sec. at 71.89% span)	$\geq$	9.6%
t/c (sec. at 83.07% span)	$\geq$	9.5%
t/c (sec. at 94.14% span)	$\geq$	9.5%

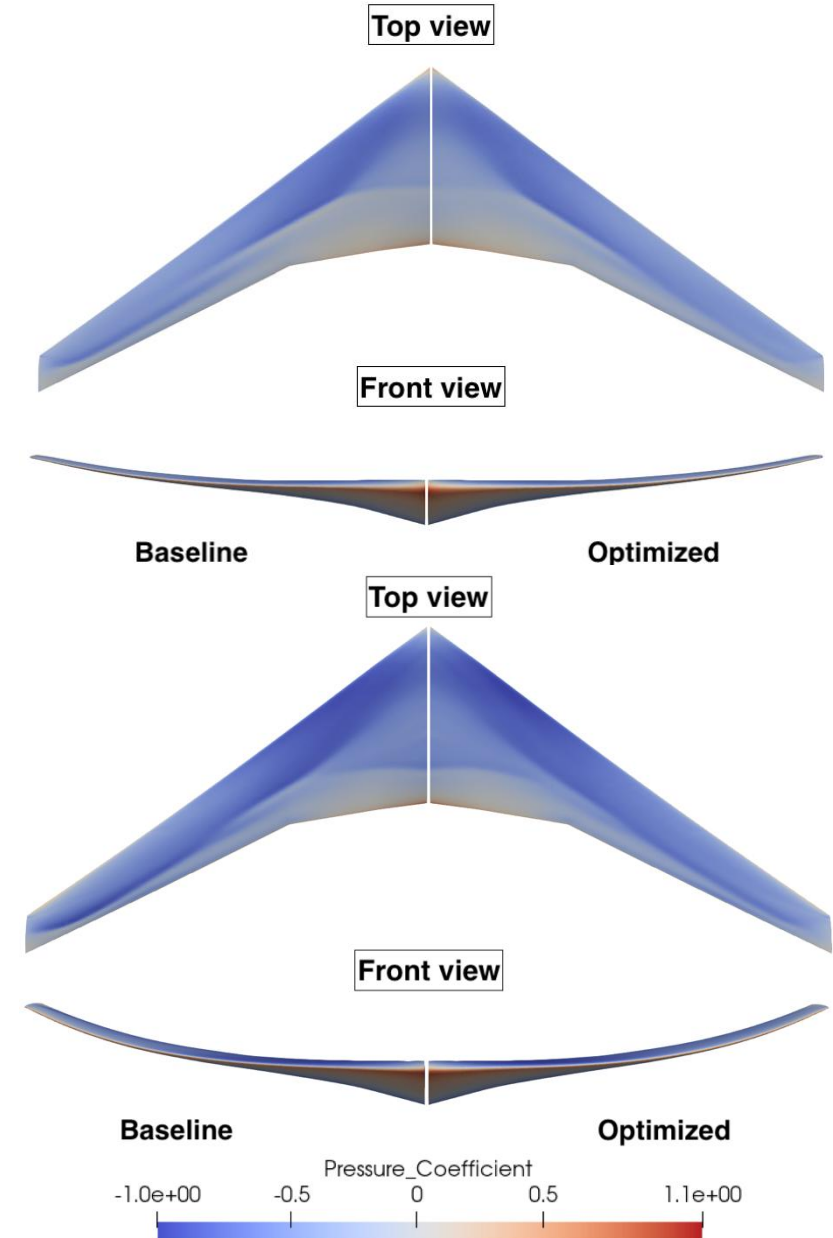
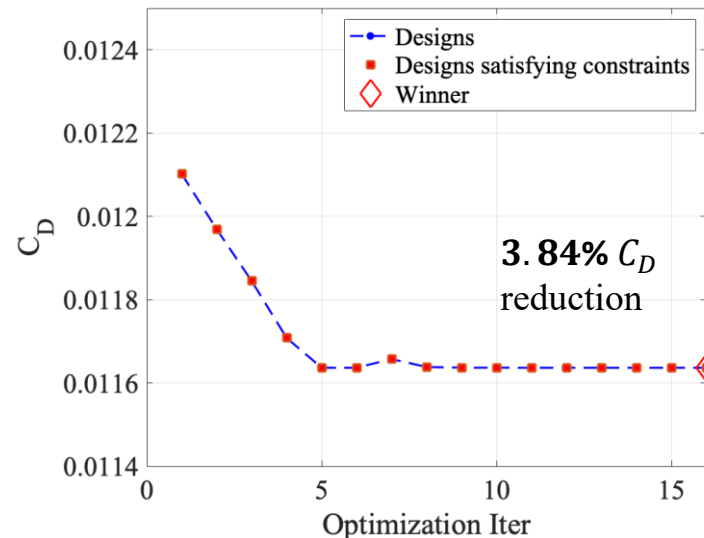
$$\text{Number of DVs} = 418$$

### Optimization results

#### AWSO (Rigid wing)



#### ASWSO (aerostructural)



## AWSO and ASWSO comparison

Configuration	$C_D$	Diff. %
ASWSO optimum	0.01163	—
AWSO optimum	0.01243	6.87%
Original	0.01210	4.04%

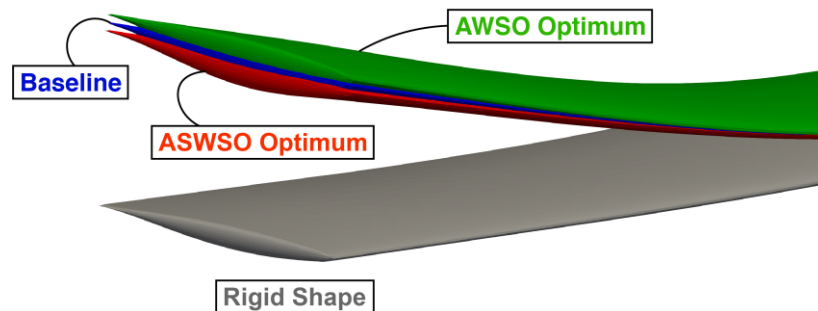
### $C_D$ comparison at aeroelastic equilibrium

**AWSO** optimum performs **worse** than the ASWSO.

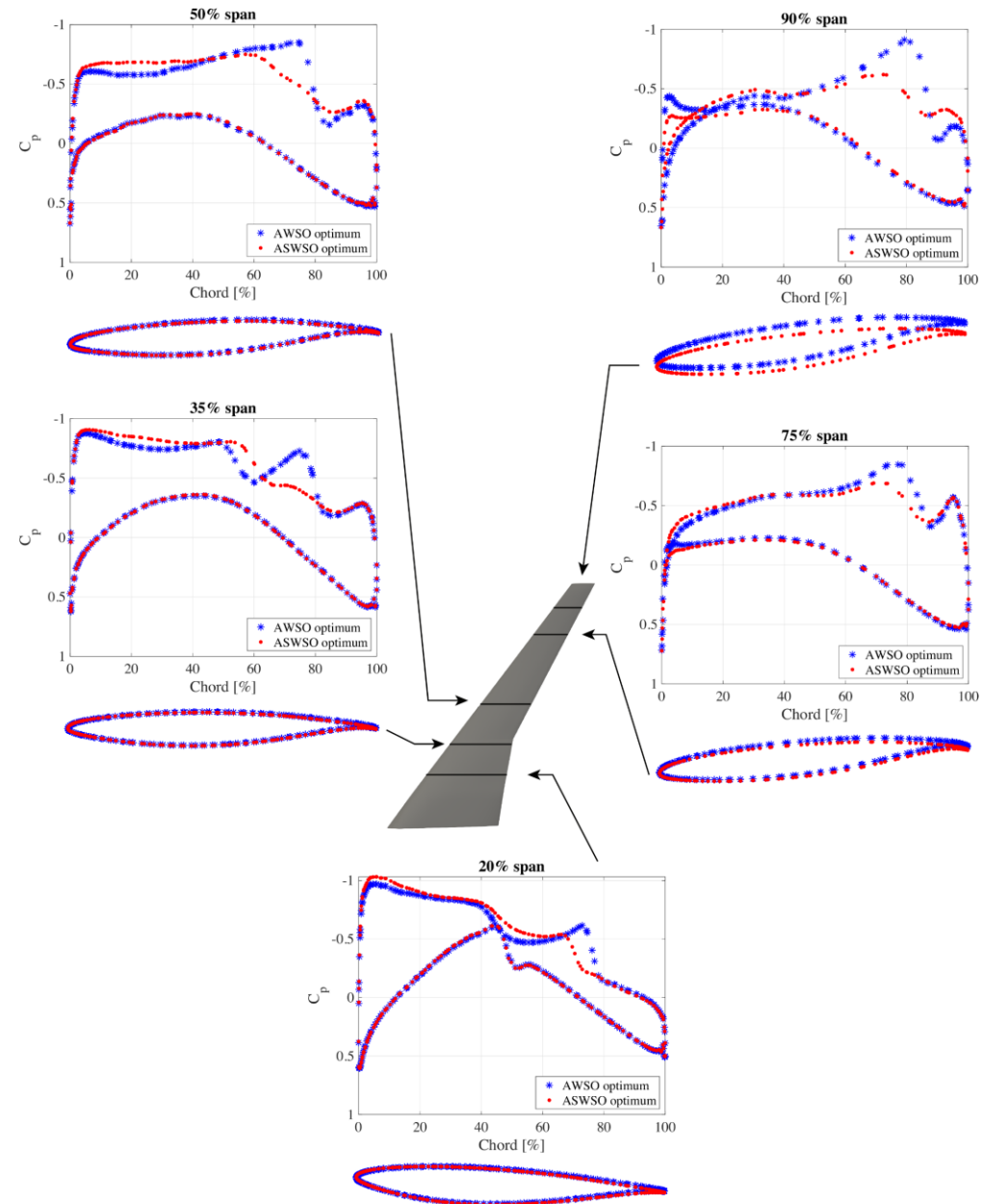
- Optimized for an **off-design** point.

**AWSO** optimum performs **worse** than the baseline.

For highly flexible wings AWSO doesn't necessarily payback.



Flying shapes comparison



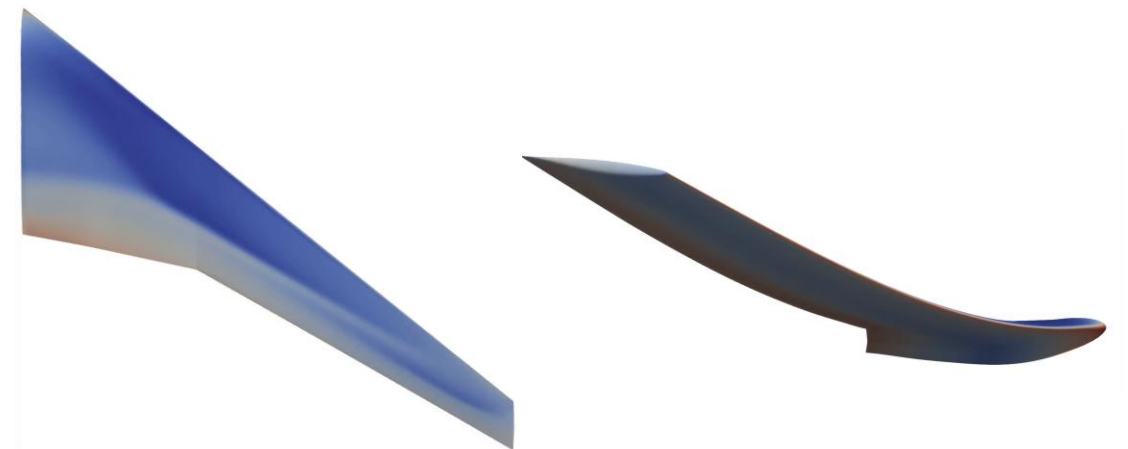
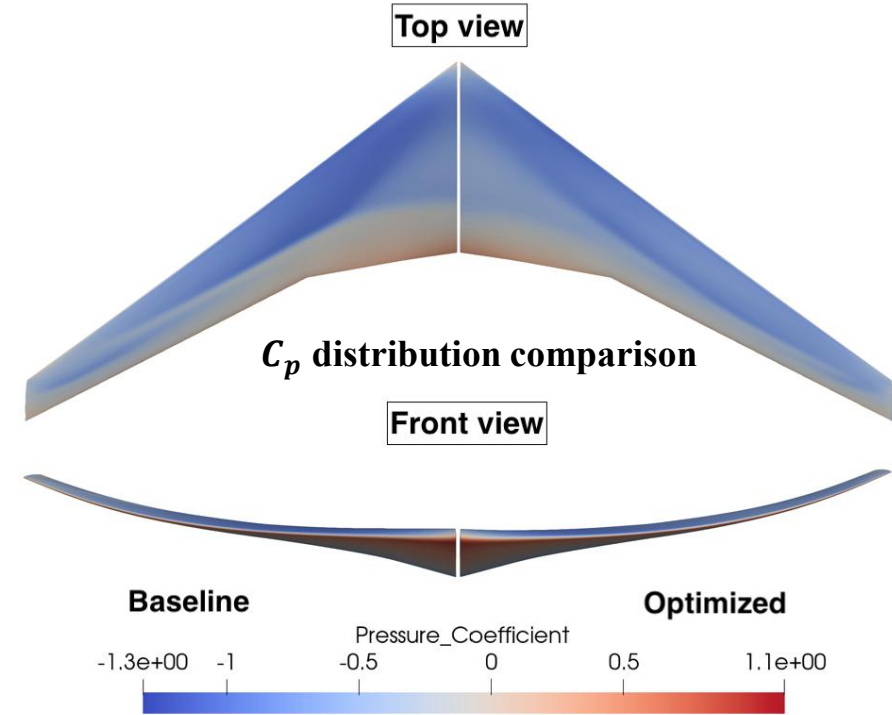
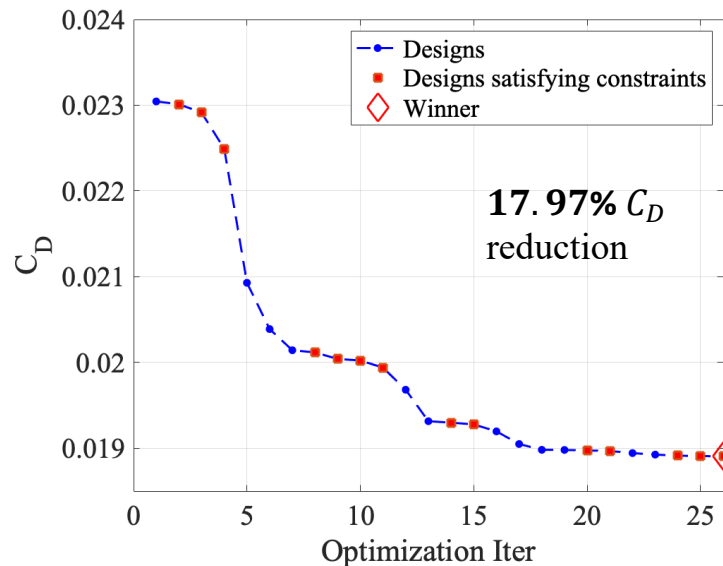
AWSO and ASWSO flying shapes  $C_p$  distribution comparison

## Optimization of the CRM (RANS-SA)

### ASWSO (aerostructural)

- **Ideal gas** model.
- **Laminar** viscosity with **Sutherland's** law.
- **Turbulent** viscosity with **SA** one equation.
- **Full-turbulence** (non-frozen turbulence) adjoint.
- Same aerodynamic and geometric constraints.

### Optimization results





## Optimization of the very-flexible CRM (Euler)

### ASWSO (aerostructural)

#### Aerodynamic constraints

$$C_L = 0.5$$

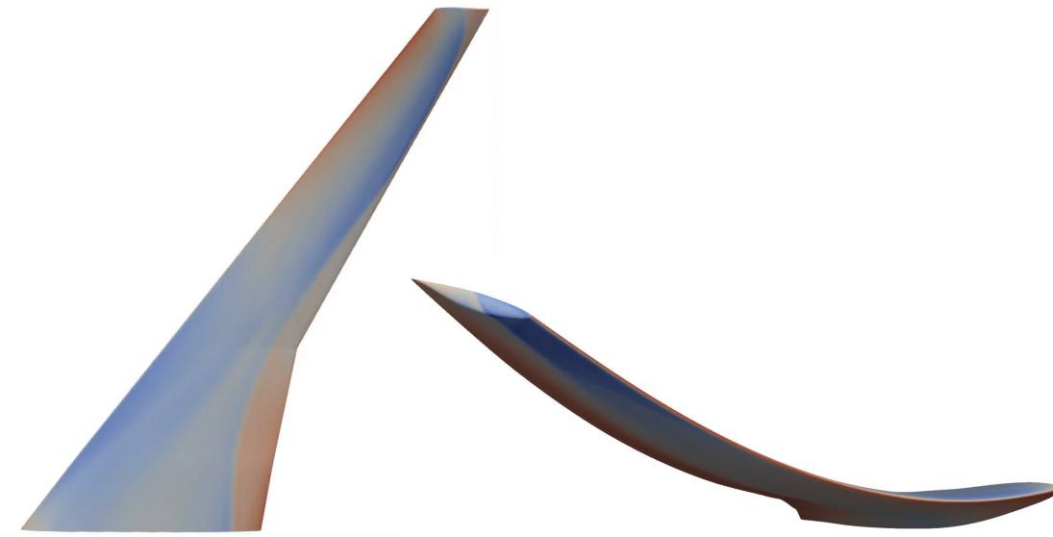
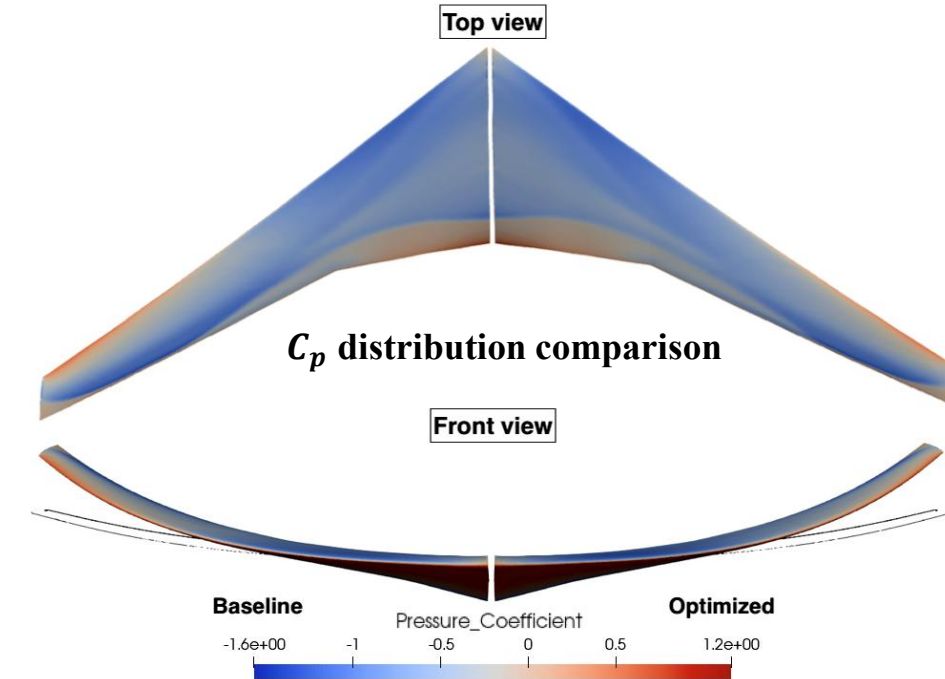
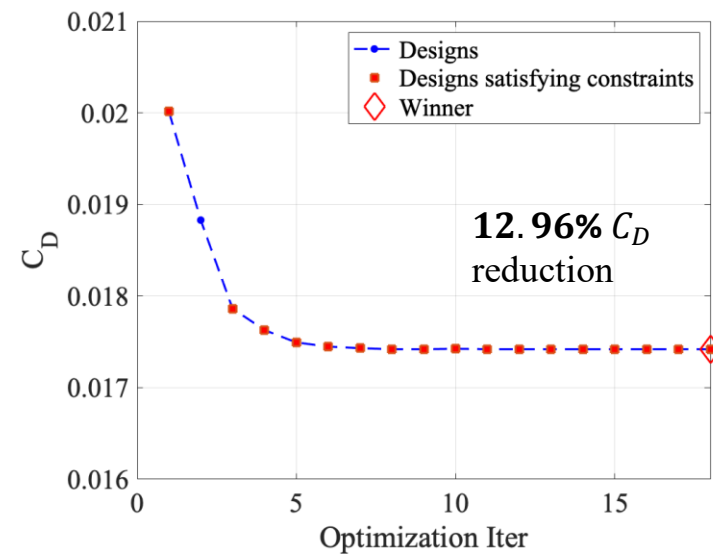
#### Geometric constraints

t/c (sec. at 0.34% span)	$\geq$	15.6%
t/c (sec. at 16.32% span)	$\geq$	12.5%
t/c (sec. at 27.01% span)	$\geq$	11.2%
t/c (sec. at 38.49% span)	$\geq$	10.4%
t/c (sec. at 49.76% span)	$\geq$	10.0%
t/c (sec. at 60.74% span)	$\geq$	9.8%
t/c (sec. at 71.89% span)	$\geq$	9.6%
t/c (sec. at 83.07% span)	$\geq$	9.5%
t/c (sec. at 94.14% span)	$\geq$	9.5%

$$\text{Number of DVs} = 418$$

Wing stiffness tuned to have **~14%** of semi-span wing tip deflection at aeroel. equilibrium.

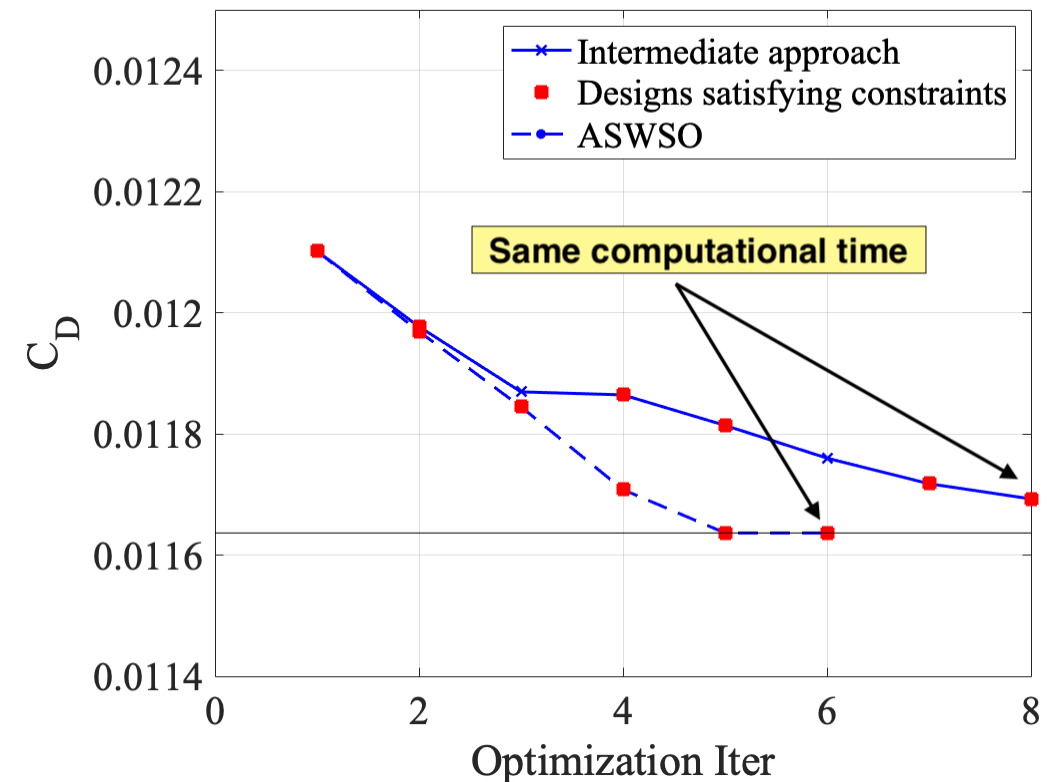
### Optimization results



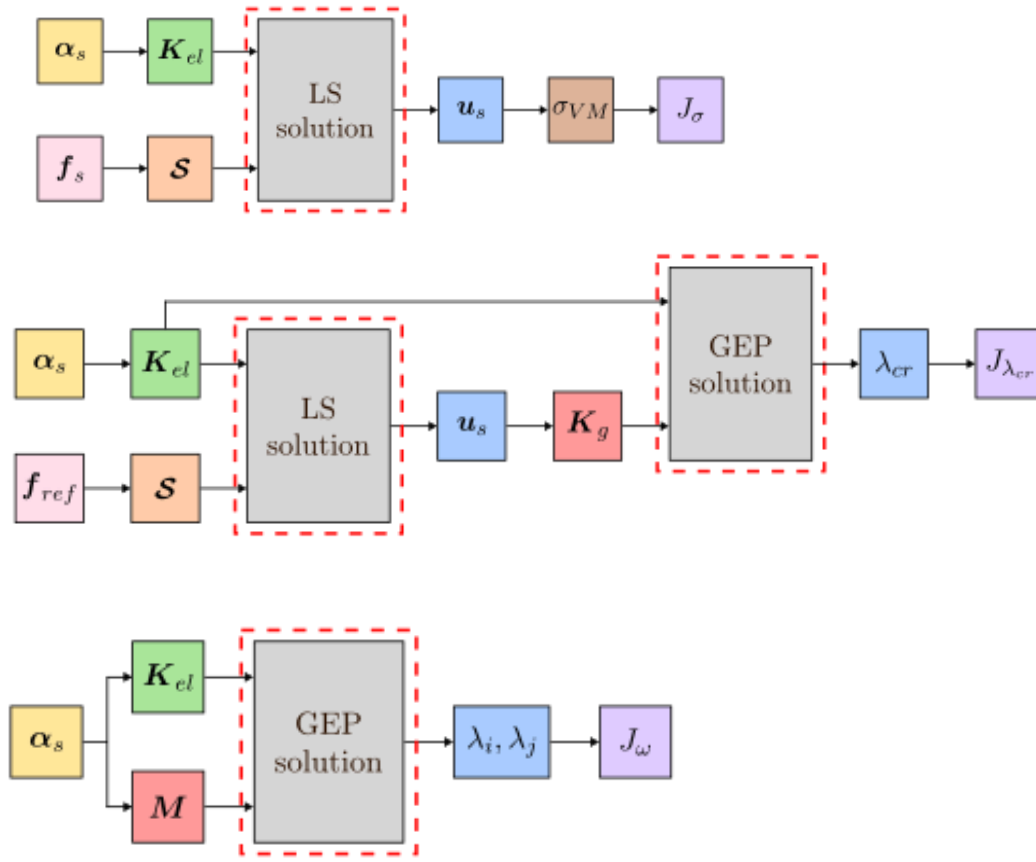
## Coupled gradients vs uncoupled gradients

### ASWSO (aerostructural)

- **Fully-coupled** approach (coupled primal and adjoint problem)
  - Discrete-exact gradients
  - More complex; gradient evaluation more costly
- Intermediate approach: gradients **without** **aerostructural coupling**
  - Inexact gradients
  - Simpler; cheaper gradient evaluation
- For a given **computational budget**, **fully-coupled** approach is providing a better result
- For more flexible wing, the approximated gradient can be too imprecise, and determine failure of the optimization problem.



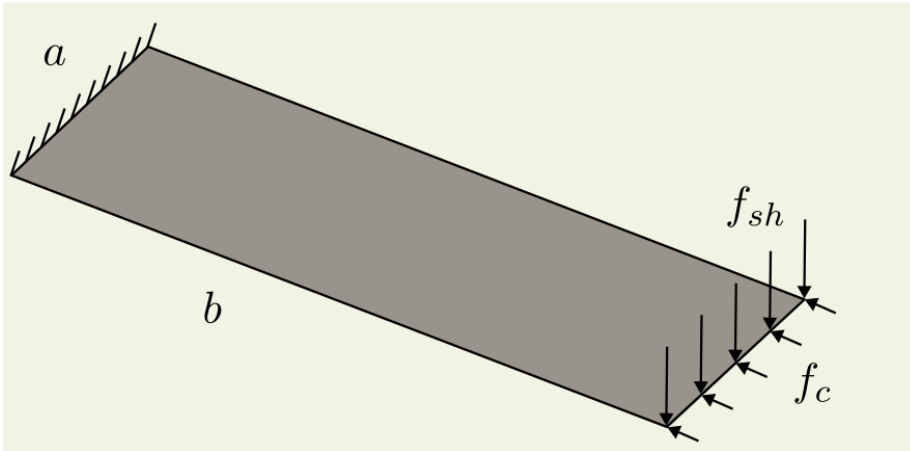
- Improvement of FE solver.
- AD-based adjoints
  - Stresses
  - Buckling
  - Free Vibration modes (step towards flutter)



Governing equations	$c_i \leq 0$
$S = K_{el} u_s - f_s = 0$	$J_\sigma = KS(g_i) = \frac{1}{\rho_{KS}} \log \sum_{i=1}^n e^{\rho_{KS} \cdot g_i} \leq 0$ (where $g_i = \frac{\sigma_i^{VM}}{\sigma_{ADM}} - 1$ )
$(K_{el} - \omega_k^2 M) \phi_k = 0$	$J_\omega = \rho_\omega \frac{(\omega_j - \omega_i)_{init}}{\omega_j - \omega_i} - 1 \leq 0$
$(K_{el} + \lambda_k^{cr} K_g) \phi_k^{cr} = 0$	$J_{\lambda_{cr}} = \rho_{\lambda_{cr}} \frac{(\lambda_1^{cr})_{init}}{\lambda_1^{cr}} - 1 \leq 0$

	Primal problem	Adjoint statement
Linear system	$K_{el} u_s = f_s$	$K_{el}^T s = \frac{\partial J}{\partial u_s}$ $\bar{K}_{el} += -s \cdot u_s$ $\bar{s} += s$
Generalised eigenvalue problem	$A \phi_k = \lambda_k B \phi_k$	$\bar{A} += \phi_k \phi_k^T$ $\bar{B} += -\lambda_k \bar{A}$

# Structural optimisation – testcase 1



- **8 DVs:**  $\alpha_{s,0} = 5.0 \text{ mm}$ ;  $1.0 \text{ mm} \leq \alpha_{s,i} \leq 10.0 \text{ mm}$

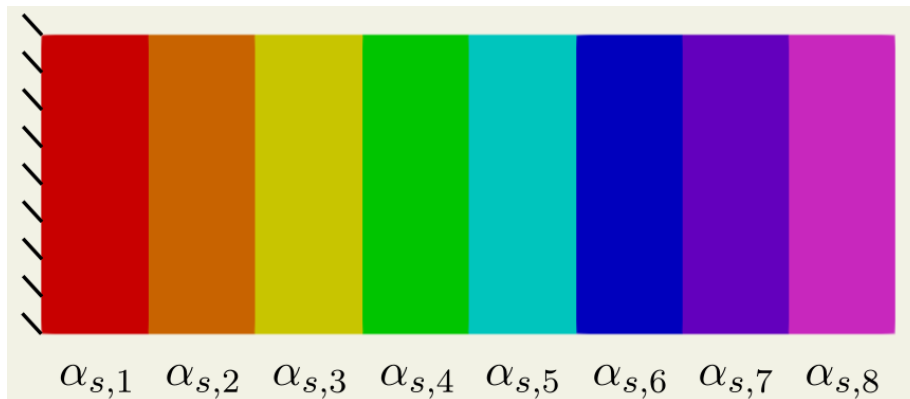
- **4 optimisation runs for 4 constraint sets:**

**1. Stress:**  $\sigma_{VM}$  aggregated on all elements;  $\sigma_{ADM} = 270 \text{ MPa}$

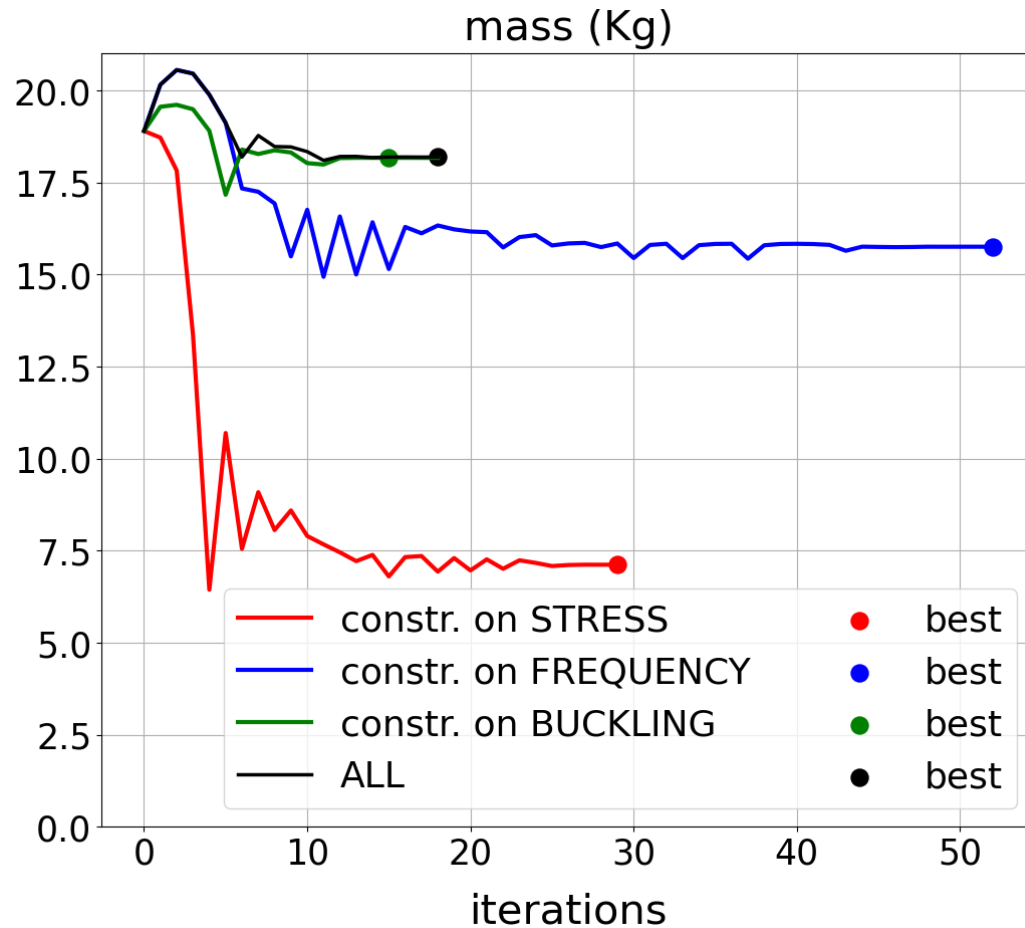
**2. Frequency:**  $(\omega_2 - \omega_1) \geq 1.2 * (\omega_2 - \omega_1)_{init}$

**3. Buckling:**  $\lambda_1^{cr} \geq 1.2 * (\lambda_1^{cr})_{init}$

**4. All:** stress + frequency + buckling together



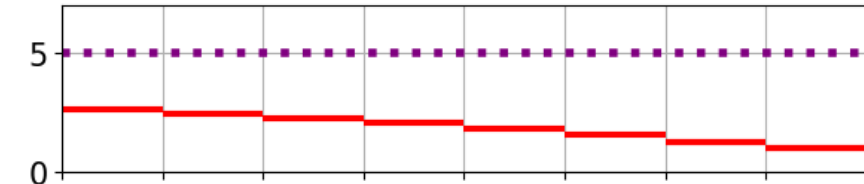
# Structural optimisation - testcase 1 - results



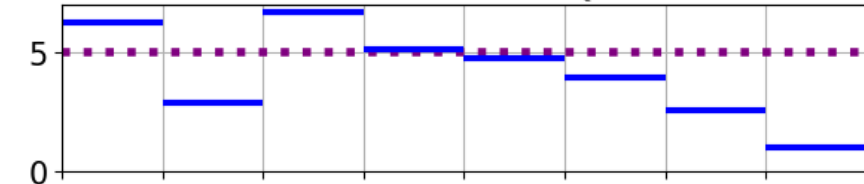
Constraint	Stress	Frequency	Buckling	all
M (Kg)	7.12	15.76	18.17	18.19
$\Delta m$ (%)	-62.33	-16.61	-3.86	-3.76

## Optimal thickness distribution (mm)

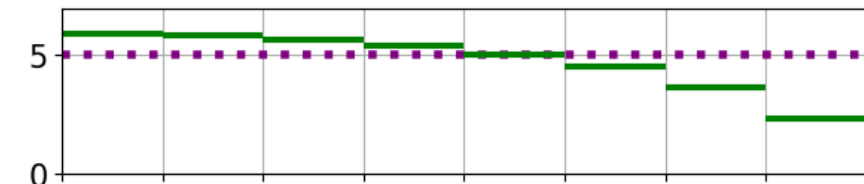
Constraint on STRESS



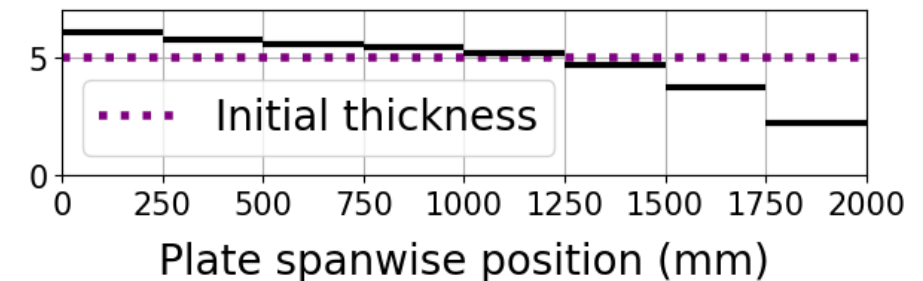
Constraint on FREQUENCY



Constraint on BUCKLING

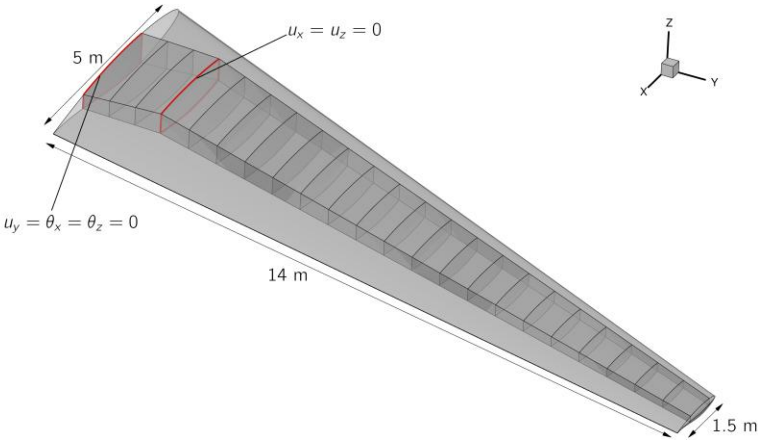


ALL



# Structural optimisation - testcase 2

## High-Fidelity Aeroelastic Optimisation Benchmark



- rib nodes loaded along the z direction; root & fus. intersection constr.
- **111 DVs** :  $\alpha_{s,ini} = 7.0$  mm;  $1.0 \text{ mm} \leq \alpha_{s,i} \leq 20.0$  mm
- **3 optimisation runs for 3 constraint sets:**

### 1. Stress constraint set: 5 aggregation areas

RIBS

FRONT SPAR

REAR SPAR

TOP SKIN

BOTTOM SKIN

$$\sigma_{ADM} = 320 \text{ Mpa}$$

Imposed simultaneously  
(5 constraints)

### 2. Frequency constraint

$$(\omega_2 - \omega_1) \geq \rho_\omega (\omega_2 - \omega_1)_{ini}$$

$$\rho_\omega = 1$$

$$(\omega_3 - \omega_2) \geq \rho_\omega (\omega_3 - \omega_2)_{ini}$$

$$\rho_\omega = 1$$

$$\omega_1 \geq \rho_\omega (\omega_1)_{ini}$$

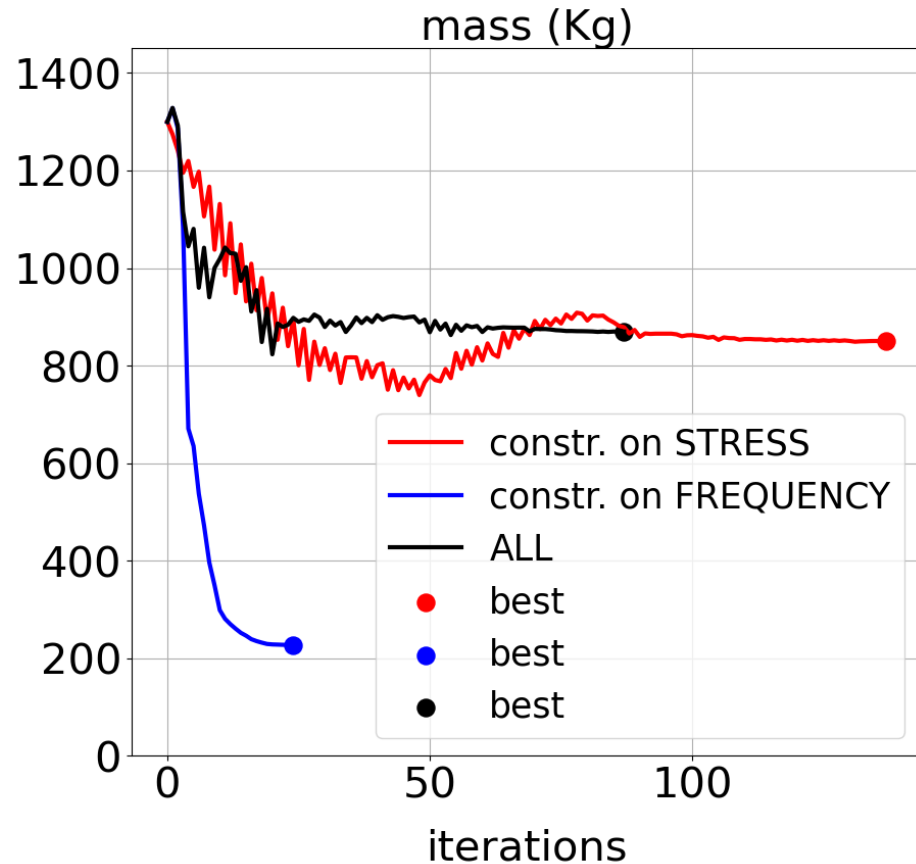
$$\rho_\omega = 1.15$$

Imposed simultaneously  
(3 constraints)

### 3. Mixed ("All") constraint set: stress + frequency constraint sets together (8 in total)



# Structural optimisation - testcase 2 - results

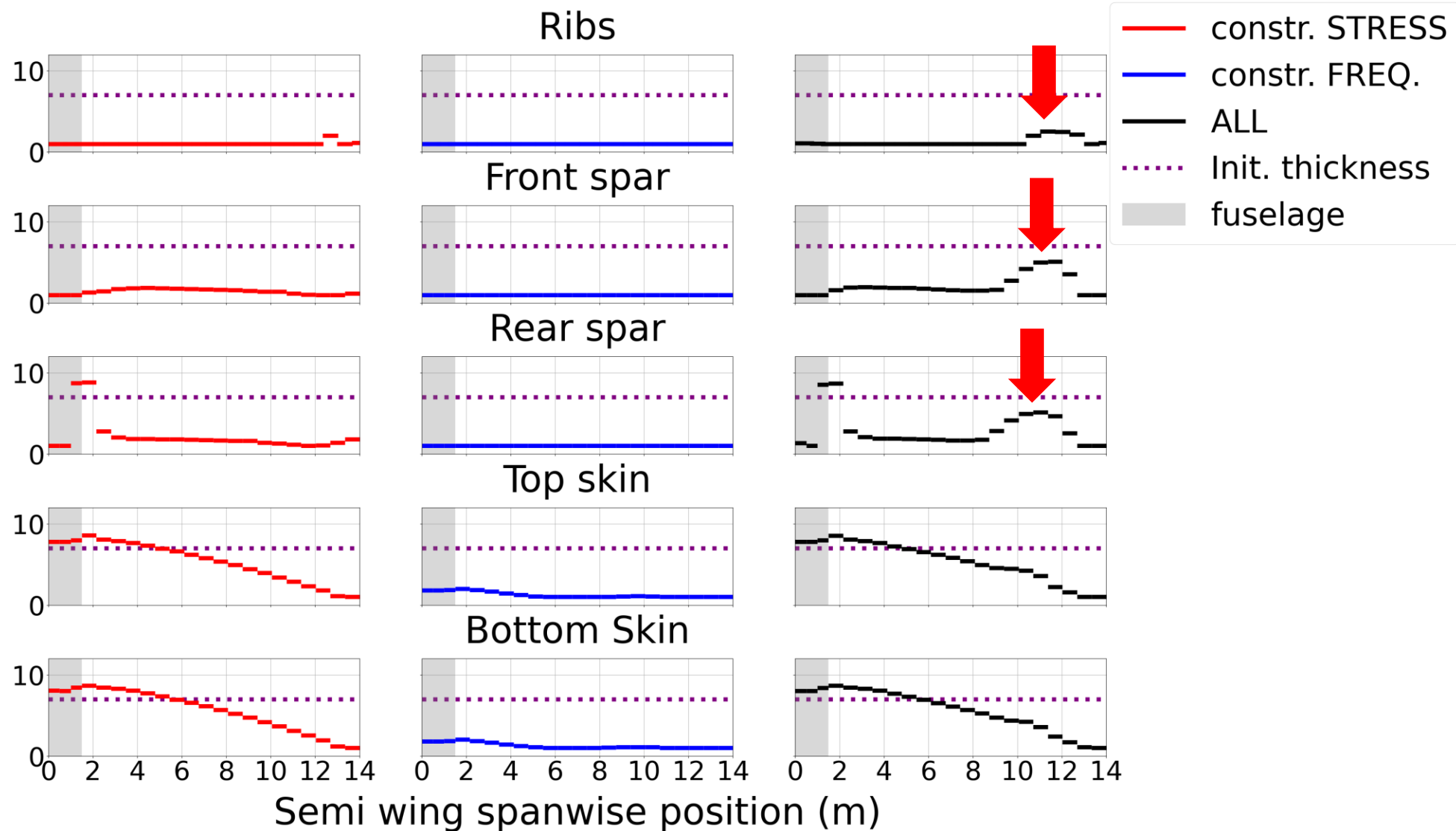


Constraint	Stress	Frequency	all
M (Kg)	850.17	227.58	869.91
$\Delta m$ (%)	-34.58	-82.49	-33.06

Active constraints			
	Constr. on STRESS	Constr. on FREQUENCY	ALL
$J_{\sigma}^{RIBS}$	Active	Inactive	Active
$J_{\sigma}^{FSPAR}$	Active	Inactive	Active
$J_{\sigma}^{RSPAR}$	Active	Inactive	Active
$J_{\sigma}^{TSKIN}$	Active	Inactive	Active
$J_{\sigma}^{BSKIN}$	Active	Inactive	Active
$J_{\omega}^{(\omega_1)}$	Inactive	Active	Inactive
$J_{\omega}^{(\omega_2 - \omega_1)}$	Inactive	Active	Inactive
$J_{\omega}^{(\omega_3 - \omega_2)}$	Inactive	Active	Inactive

# Structural optimisation - testcase 2 - results

Optimal spanwise thickness distribution (mm)



17 July 2025

University of Kaiserslautern-Landau

# Multidisciplinary Design Optimization for Next-Generation Sustainable Aircraft

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